

The shape of velocity dispersion profiles and the dynamical state of galaxy clusters

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ABSTRACT

Motivated by the existence of the relationship between the dynamical state of clusters and the shape of the velocity dispersion profiles (VDPs), we study the VDPs for Gaussian (G) and non-Gaussian (NG) systems for a subsample of clusters from the Yang catalogue. The groups cover a redshift interval of $0.03 \leq z \leq 0.1$ with halo mass $\geq 10^{14} M_{\odot}$. We use a robust statistical method, Hellinger Distance, to classify the dynamical state of the systems according to their velocity distribution. The stacked VDP of each class, G and NG, is then determined using either Bright or Faint galaxies. The stacked VDP for G groups displays a central peak followed by a monotonically decreasing trend which indicates a predominance of radial orbits, with the Bright stacked VDP showing lower velocity dispersions in all radii. The distinct features we find in NG systems are manifested not only by the characteristic shape of VDP, with a depression in the central region, but also by a possible higher infall rate associated with galaxies in the Faint stacked VDP.

Key words: galaxies: clusters: general.

1 INTRODUCTION

In a hierarchical universe (Λ cold dark matter, Λ CDM), galaxy clusters constitute the last representative blocks of the large-scale structures to be formed by accretion of lower mass systems from the general field and filamentary regions (e.g. Gunn & Gott 1972; Press & Schechter 1974; White & Frenk 1991; Ebeling, Barrett & Donovan 2004). In this scenario, clusters represent the most massive structures recently collapsed in the universe and also the most dynamically ‘immature’ (e.g. Boylan-Kolchin et al. 2009; Iliev et al. 2010). An important tracer of the dynamical state of galaxy clusters, is the velocity dispersion profile (e.g. Struble 1979), which provides valuable information on the degree of anisotropy of galaxy orbits and is also related to the cluster density profile (e.g. Jing & Borner 1996; Biviano et al. 1997; Adami, Biviano & Mazure 1998). Menci & Fusco-Femiano (1996), after numerically integrating the Boltzmann–Liouville equation for colliding galaxies in the potential well of clusters, find that centrally increasing or decreasing VDPs are associated with the balance between galaxy interactions and the shape of the dark matter distribution. Using the CNOC1 survey, Carlberg et al. (1997) show that velocity dispersion rises from 0.1 virial radius, reaches a peak around 0.3 virial radius and then presents a roughly flat profile with a very slight de-

cline (see also van der Marel et al. 2000). With a different approach, studying the kinematics of groups in the SDSS DR7, Li et al. (2012) find that the average velocity dispersion within the virial radius is a strongly increasing function of the central galaxy mass. Generally, increasing or decreasing features of VDPs could be related to the influence of cD galaxies in the first radial bin, two-body relaxation and orbit circularization in the central region of clusters (den Hartog & Katgert 1996; Girardi et al. 1998). In other words, a critical factor influencing the shape of the VDPs is the dynamical state of clusters (e.g. den Hartog & Katgert 1996; Hou et al. 2009; Pimblet, Penny & Davies 2014).

Although galaxy clusters may go through different dynamical states, they are usually classified in only two classes: relaxed and unrelaxed (e.g. Hou et al. 2009; Ribeiro, Lopes & Trevisan 2011; Cui et al. 2017). Dynamically relaxed clusters are expected to have Gaussian line-of-sight velocity distributions (e.g. Yahil & Vidal 1977; Bird & Beers 1993; Ribeiro et al. 2013), while unrelaxed systems present significant departures from the Gaussian distribution, which can be seen as evidence of different ongoing physical processes: presence of interlopers; displacement of the brightest cluster galaxy (BCG) from the peak of the projected galaxy density, or from the peak of the X-ray emission; circular orbits; and the most frequent, the presence of substructures (e.g. Beers & Geller 1983; Lin & Mohr 2004; Owers, Couch & Nulsen 2009; Lauer et al. 2014; Rossetti et al. 2016). All these effects reinforce the idea that the shape of the VDPs can be assessed by investigating the dynamical state of galaxy clusters. Hou et al. (2009),

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using a sample selected from CNOC2, find that the VDPs of groups with non-Gaussian velocity distribution are significantly different from the Gaussian ones. Also, Hou et al. (2012) studying groups of intermediate redshift from the Group Environment and Evolution Collaboration (GEEC) catalogue, show that there is a relationship between the shape of the VDPs and the presence of substructures in clusters. Using the methodology prescribed by Bergond et al. (2006) to compute the VDPs, they notice that all groups with substructures have strictly increasing VDPs.

All these studies not only show the importance of the use of VDPs as a proxy of the dynamical state of clusters, but also point to a possible relationship, between their behaviour and the different physical mechanisms in action within clusters. In previous studies, the shape of VDPs was analysed considering a number of dynamical indicators (e.g. Menci & Fusco-Femiano 1996; Hou et al. 2009). In this Letter, we study the VDPs of 177 groups selected by de Carvalho et al. (2017) from the Yang catalogue (Yang et al. 2007), taking into account the dynamical state of the groups based on a robust statistical method (Section 2.2). We describe the sample used in Section 2. The results obtained for the VDPs are presented in Section 3 followed by a discussion in Section 4. Throughout this work, we assume a Λ CDM cosmology with $\Omega_M = 0.3$, $\Omega_\Lambda = 0.7$ and $H_0 = 100 \text{ km s}^{-1} \text{ Mpc}^{-1}$.

2 DATA AND METHODOLOGY

In this section, we will briefly describe the sample and the procedures used to identify the dynamical state of the groups. For more details on the sample and dynamical classification, see de Carvalho et al. (2017).

2.1 Yang groups

To study the VDPs of Yang groups, we use an updated sample of Yang catalogue (Yang et al. 2007) presented by de Carvalho et al. (2017) based on 593 736 galaxies from SDSS-DR7 (York et al. 2000), supplemented with additional 3 115 galaxies with redshifts from different sources. The galaxies from SDSS-DR7 covers an interval of $0.03 \leq z \leq 0.1$ and r magnitudes brighter than 17.78 (spectroscopic completeness limit of the survey), ensuring that we cover the luminosity function up to $M^* + 1$ for all systems. The membership, R_{200} , M_{200} and velocity dispersion for each group were re-estimated by shift-gapper technique and virial analysis following prescription described in Lopes et al. (2009). Finally, only systems with more than 20 galaxies within R_{200} are used. After these constraints in redshift ($0.03 \leq z \leq 0.1$) and richness, the number of groups/clusters remaining is 319.

2.2 Classifying the dynamical state of groups

To classify the dynamical state of the 319 groups/clusters we use a new method, Hellinger distance (HD), which is based on their line-of-sight velocity distribution. Succinctly, HD (Le Cam & Yang 2012) measures how far from a Gaussian a given distribution is. It was first introduced in astronomy by Ribeiro et al. (2013), studying the degree of Gaussianity of the velocity distribution of galaxies in Berlind's groups (Berlind et al. 2006). We estimate HD using codes available in R environment under the distrEx package (Ruckdeschel 2006). Only Gaussian (G) or non-Gaussian (NG) systems with reliability greater than 70 per cent were considered (see de Carvalho et al. 2017 for details). Also, we find that, through the relation between M_{200} and N_{R200} (where N_{R200} is the number of

galaxies within R_{200} with $M_r \leq -20.55$), a mass cutoff of $10^{14} M_\odot$ corresponds to $N_{R200} = 20$. These constraints define a final sample of 177 groups/clusters, being 143 G and 34 NG. Also, in the analysis that follows, we consider two specific domains of luminosity for the final sample: bright, using galaxies with $M_r \leq -20.55$, probing the systems up to $M^* + 1$ (Blanton et al. 2001); Faint, using galaxies with $-20.55 < M_r \leq -18.40$. The faint domain is only analysed for groups/clusters in the range $0.03 \leq z \leq 0.04$, examining the luminosity function down to $\sim M^* + 3$.

3 VELOCITY DISPERSION PROFILES ANALYSIS

The study of VDPs is a powerful tool for doing dynamical analysis of galaxy clusters (e.g. Struble 1979; den Hartog & Katgert 1996; Pimblet et al. 2014). We probe the VDPs for clusters classified as G and NG, first using all galaxies and then exploring both luminosity domains previously defined. We estimate the cumulative velocity dispersion with the robust bi-weight scale estimator described by Beers, Flynn & Gebhardt (1990), instead of the methodology presented by Bergond et al. (2006). This method requires a careful choice of the kernel scale parameter which is very sensitive, namely, for large values some VDP features may disappear, while choosing small values tend to add fake components to VDPs. Different choices of the kernel parameter and their effects are detailed in Hou et al. (2009) and Pimblet et al. (2014).

Subsequently, we build composite clusters, since this is the most appropriate way to investigate galaxies in multiple galaxy systems (Biviano & Girardi 2003; Ribeiro, Lopes & Trevisan 2010). Also, by using composite clusters, we reduce asymmetries in the galaxy distribution (Biviano 2001). We create two composite groups, G (composed of 143 systems) and NG (composed of 34 systems). The stacked VDPs (SVDPs) for these two classes have distances to the group centre normalized by R_{200} and their peculiar velocities are scaled to the cluster velocity dispersion. VDPs are obtained by ordering the members of the stacked cluster in distance and measuring the scale within the radius of each galaxy considered in each step starting with the first 10 galaxies ordered in distance, since this number of galaxies corresponds to an efficiency between 70 per cent and 80 per cent of the estimates obtained by the bi-weight estimator (Beers et al. 1990) and are also sufficient to obtain an unbiased estimate of a cluster dispersion (Biviano et al. 2006). Fibre collision problem can be an issue when measuring galaxy clustering statistics on small scales and for that reason we estimate that the radius within which the effect can be important is $0.15h^{-1} \text{ Mpc}$ (55 arcsec). With a typical R_{200} (evaluated from the 319 clusters) of $0.95h^{-1} \text{ Mpc}$, we distrust measurements within $R_p/R_{200} \sim 0.16$.

In Fig. 1, we plot the SVDPs for G groups, σ/σ_{M200} , as a function of R_p/R_{200} , where σ_{M200} represents the estimated velocity dispersion measured by the shift-gapper technique (Lopes et al. 2009). From this figure, we clearly see that velocity dispersion increases to approximately $R_p/R_{200} \sim 0.35$, and for larger radii the profile is monotonically decreasing. For NG clusters, Fig. 2, we see that the shape of the SVDP exhibits a central depression and then increases from $R_p/R_{200} \sim 0.5$ to 1.0. This upward trend is also observed in two NG groups studied by Hou et al. (2009), which is interpreted as a signature of merge by Menci & Fusco-Femiano (1996).

These differences between SVDPs for G and NG groups make it more evident that these systems are in different stages of evolution. In the SVDP for G groups, we see an increase up to $R_p/R_{200} \sim 0.35$, which might indicate a cool core remnant, characteristic of

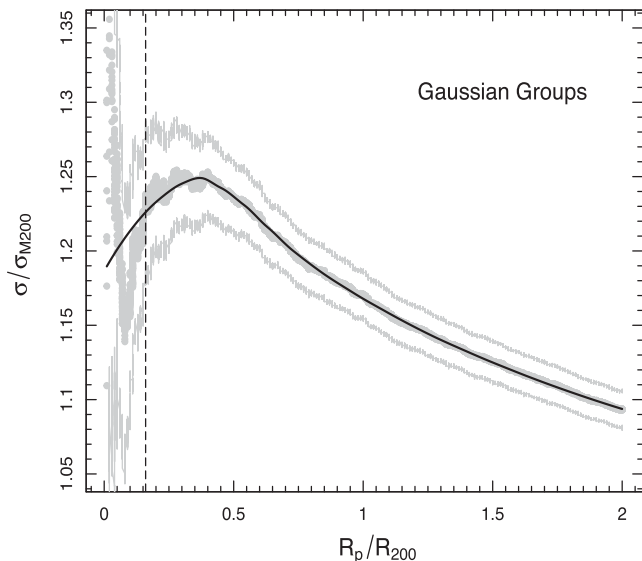


Figure 1. SVDP for clusters classified as G. The grey points represent the velocity dispersion estimated in each R_p/R_{200} considered and the solid black line represents the best Locally Weighted Scatterplot Smoothing (LOWESS) estimates to the all galaxies along the profile. The grey lines are representative of the confidence intervals (90 per cent) obtained through 1000 bootstraps, and the vertical dashed line represents the inner radius to which the fibre collision problem can be considered.

relaxed systems, originating from a process of violent relaxation as noticed by Dressler & Shectman (1988) and den Hartog & Katgert (1996). This tendency for relaxed systems is also consistent with the results presented by Girardi et al. (1998) and Cava et al. (2017), who find similar behaviour for a stacked sample of clusters classified as regular using the Dressler-Schetman test (Dressler & Shectman 1988). In regions external to $R_p/R_{200} \sim 0.35$, the SVDP decreases, as expected for G systems (without substructures), i.e. in regions where there is a predominance of radial orbits (e.g. Natarajan, Hjorth & van Kampen 1997). As for the SVDP of NG systems, the depression seen in the central region, internal to $R_p/R_{200} \sim 1.0$, suggests that subgroups of galaxies may be in some stage of

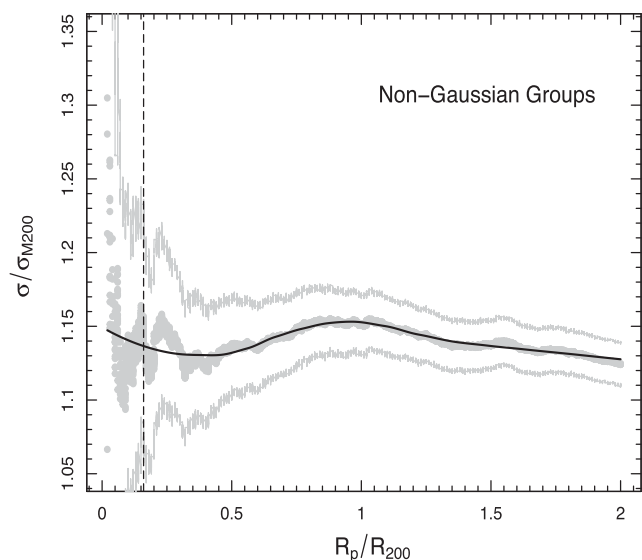


Figure 2. SVDP for clusters classified as NG. The points and lines (grey and black) have the same meaning as those explained in Fig. 1.

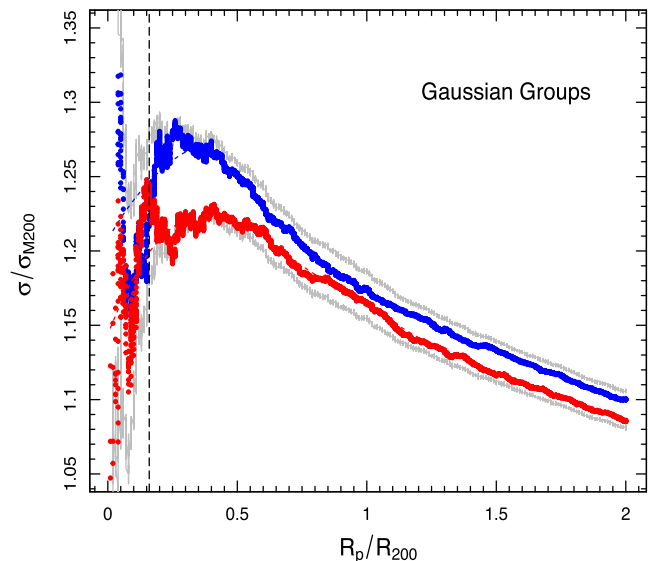


Figure 3. VDP for G systems with superposition of profiles for galaxies classified as Bright (red) and Faint (blue). Both profiles are within the confidence envelope obtained through all objects in this sample.

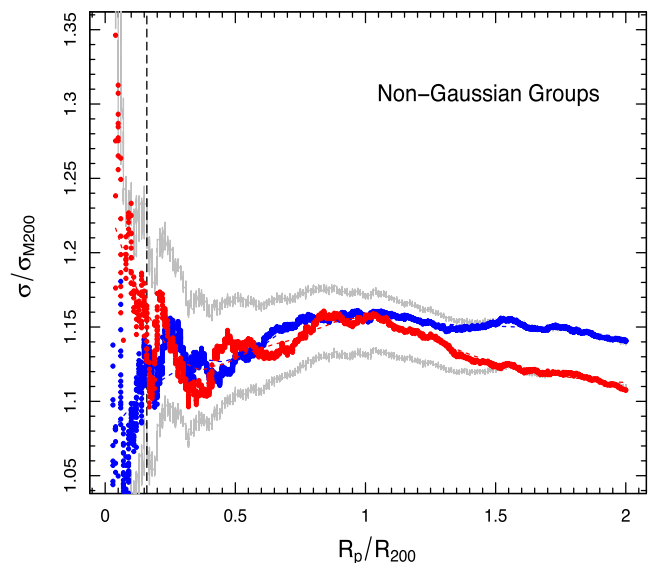


Figure 4. VDPs for the Bright and Faint populations belonging to the NG sample. The profiles blue and red represent the two domains of luminosity considered.

merging, a scenario consistent with the absence of a cool dense core, which allows substructures penetrate deep inside the potential well and disturb the cluster central dynamics (Churazov et al. 2003; Ribeiro et al. 2011). Finally, for regions with $R_p/R_{200} \gtrsim 1.0$, the SVDP becomes slightly flat, suggesting that the measured velocity dispersion at larger radii is more representative of the total kinetic energy of the cluster galaxies (e.g. Fadda et al. 1996; Biviano & Girardi 2003; Zhang et al. 2011).

We extend our analysis of the SVDPs to the two luminosity domains, Bright and Faint, and two dynamical classes, G and NG as displayed in Figs 3 and 4. For reference, we superimpose the SVDPs obtained when all galaxies are used. The red and blue profiles represent the SVDPs measured using only the Bright and Faint galaxies, respectively. Both profiles are inside the confidence envelope for G

and NG groups, indicating that their characteristics do not reflect unphysical effects.

In Fig. 3, we see that the Bright and Faint SVDPs follow the same general trend: the Bright component exhibits a lower velocity dispersion with respect to the Faint one along the entire profile, as also obtained by Goto (2005) ($M_z < -23.0$) and for bright objects ($M_R \leq -21.5$) in G groups by Ribeiro et al. (2010). Results from Aguerra, Sánchez-Janssen & Muñoz-Tuñón (2007), considering the brightest galaxies ($M_r < -21.0$) for their sample of 88 nearby galaxy clusters from SDSS-DR4, seem to corroborate this trait. In Fig. 4, we notice that up to $R_p/R_{200} \sim 1.0$ the SVDP is not only considerably reduced with respect to what we find for G systems but also seem to be indistinguishable for both luminosity regimes. This behaviour reinforces the fact that NG clusters are dynamically distinct and less evolved than the G ones. In this case, we do not see any significant segregation in the inner region as we found for G clusters. However, for $R_p/R_{200} > 1.0$, the Faint SVDP predominates over the Bright one. A possible interpretation for this effect is that the Faint SVDP may be manifesting a larger number of infalling galaxies (e.g. Colín, Klypin & Kravtsov 2000). This view agrees with the results of Mahajan, Mamon & Raychaudhury (2011) who have shown that within 1.0–2.0 Mpc, infalling galaxies are the dominant population in phase space for certain values of line-of-sight velocities. In fact, these findings are in agreement with those encountered by other authors (e.g. Mohr et al. 1996; Mahdavi et al. 1999; Ellingson et al. 2001) who have demonstrated that groups infalling into clusters are dominated by blue, emission line galaxies with larger velocity dispersion than the red and more evolved galaxies.

4 DISCUSSION

In this Letter, we study the VDPs for a sample of 177 galaxy clusters from the Yang catalogue (Yang et al. 2007), with the main objective of finding a relation between the shape of the VDPs and the dynamical state of clusters. The dynamical state of each cluster (G or NG) is defined following a robust statistical method (Hellinger Distance), fully described in de Carvalho et al. (2017). From our analysis, important differences emerge when we compare the SVDPs behaviour in G and NG groups.

(i) First, the shape of the SVDP of G groups shows the characteristic behaviour of quiescent systems, with a peak corresponding to the central regions that already underwent violent relaxation, and now present cool cores with galaxies in isotropic orbits following a Gaussian distribution function (e.g. Lynden-Bell 1967; White 1996). The peak itself and the small scale of the core (up to $R_p/R_{200} \sim 0.35$) may have evolved from interactions between galaxies, or because of adiabatic compressions caused by the accumulation of infalling matter, processes that can make the core radius be diminished with time, and the central velocity dispersion be increased (Maoz 1990).

(ii) The core of G systems is surrounded by objects in predominantly radial orbits, with decreasing velocity dispersions, indicating the existence of accreting galaxies from the cluster outskirts (e.g. Solanes et al. 2001). This general behaviour (peak + monotonic decreasing) is consistent, for example, with the work of Dressler & Shectman (1988) for Abell 1983 and DC 0428-53, clusters not showing significant substructures when the Dressler-Shectman test is applied. Equivalent results are also found by others authors: Mohr et al. (1996) studying Abell 576, a galaxy cluster with a cold core, presenting a peak associated with the velocity disper-

sion of the non-emission line galaxy sample, and the decreasing behaviour is related to the dispersion of the emission line galaxies (in this study the non-emission line galaxy sample is significantly brighter than the emission line sample); Rines et al. (2003) for Abell 496, a cluster that has a very symmetric X-ray emission, considered as relaxed in both X-rays and in the galaxy distribution by Durret et al. (2000); and Biviano & Katgert (2004) when estimating the velocity dispersion for the brightest elliptical galaxies from the ENACS survey.

(iii) Other important feature for the SVDP of G groups is the kinematical segregation between the Bright and Faint components, with the Bright stacked VDP showing lower velocity dispersions in all radii. This could be indicating that, on average, the Faint VDP is built with more recently accreted galaxies than the Bright VDP. Some authors find similar results for samples defined in terms of morphology or colour, see for instance Goto (2005) and Aguerra et al. (2007).

(iv) Finally, for the NG groups, the irregular trend of the inner SVDP up to $R_p/R_{200} \sim 1.0$, exhibiting a depression, corroborates the idea that NG systems have different VDPs when compared to Gs, possibly due to mergers and infall of subgroups in the central region. Also, the excess of the Faint SVDP over the Bright one in the outskirts of the systems, suggests a higher infall rate, probably dominated by faint objects (e.g. Rines et al. 2005; Haines et al. 2015), on to NGs.

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REFERENCES

- Adami C., Biviano A., Mazure A., 1998, *A&A*, 331, 439
 Aguerra J. A. L., Sánchez-Janssen R., Muñoz-Tuñón C., 2007, *A&A*, 471, 17
 Beers T. C., Geller M. J., 1983, *ApJ*, 274, 491
 Beers T. C., Flynn K., Gebhardt K., 1990, *AJ*, 100, 32
 Bergond G., Zepf S. E., Romanowsky A. J., Sharples R. M., Rhode K. L., 2006, *AAP*, 448, 155
 Berlind A. A. et al., 2006, *ApJS*, 167, 1
 Bird C. M., Beers T. C., 1993, *AJ*, 105, 1596
 Biviano A., 2001, in Borgani S., Mezzetti M., Valdarnini R., eds, *Tracing Cosmic Evolution with Galaxy Clusters*. Astron. Soc. Pac., San Francisco, p. 127
 Biviano A., Girardi M., 2003, *ApJ*, 585, 205
 Biviano A., Katgert P., 2004, *A&A*, 424, 779
 Biviano A., Katgert P., Mazure A., Moles M., den Hartog R., Perea J., Focardi P., 1997, *A&A*, 321, 84
 Biviano A., Murante G., Borgani S., Diaferio A., Dolag K., Girardi M., 2006, *A&A*, 456, 23
 Blanton M. R. et al., 2001, *AJ*, 121, 2358
 Boylan-Kolchin M., Springel V., White S. D., Jenkins A., Lemson G., 2009, *MNRAS*, 398, 1150
 Carlberg R. G. et al., 1997, *ApJ*, 476, L7
 Cava A. et al., 2017, *A&A*, preprint, ([arXiv:1708.08541](https://arxiv.org/abs/1708.08541))
 Churazov E., Forman W., Jones C., Böhringer H., 2003, *ApJ*, 590, 225
 Colín P., Klypin A. A., Kravtsov A. V., 2000, *ApJ*, 539, 561

- Cui W., Power C., Borgani S., Knebe A., Lewis G. F., Murante G., Poole G. B., 2017, *MNRAS*, 464, 2502
- de Carvalho R. R., Ribeiro A. L. B., Stalder D. H., Rosa R. R., Costa A. P., Moura T. C., 2017, *AJ*, 154, 96
- den Hartog R., Katgert P., 1996, *MNRAS*, 279, 349
- Dressler A., Shectman S. A., 1988, *AJ*, 95, 985
- Durret F., Adami C., Gerbal D., Pislar V., 2000, *A&A*, 356, 815
- Ebeling H., Barrett E., Donovan D., 2004, *ApJ*, 609, L49
- Ellingson E., Lin H., Yee H. K. C., Carlberg R. G., 2001, *ApJ*, 547, 609
- Fadda D., Girardi M., Giuricin G., Mardirossian F., Mezzetti M., 1996, *ApJ*, 473, 670
- Girardi M., Giuricin G., Mardirossian F., Mezzetti M., Boschin W., 1998, *ApJ*, 505, 74
- Goto T., 2005, *MNRAS*, 359, 1415
- Gunn J. E., Gott III J. R., 1972, *ApJ*, 176, 1
- Haines C. P. et al., 2015, *ApJ*, 806, 101
- Hou A., Parker L. C., Harris W. E., Wilman D. J., 2009, *apj*, 702, 1199
- Hou A. et al., 2012, *MNRAS*, 421, 3594
- Iliev I. T., Ahn K., Koda J., Shapiro P. R., Pen U.-L., 2010, preprint ([arXiv:1005.2502](https://arxiv.org/abs/1005.2502))
- Jing Y. P., Borner G., 1996, *MNRAS*, 278, 321
- Lauer T. R., Postman M., Strauss M. A., Graves G. J., Chisari N. E., 2014, *ApJ*, 797, 82
- Le Cam L., Yang G. L., 2012, *Asymptotics in Statistics: Some Basic Concepts*. Springer Science & Business Media, New York
- Li C., Jing Y. P., Mao S., Han J., Peng Q., Yang X., Mo H. J., van den Bosch F., 2012, *ApJ*, 758, 50
- Lin Y.-T., Mohr J. J., 2004, *ApJ*, 617, 879
- Lopes P. A. A., de Carvalho R. R., Kohl-Moreira J. L., Jones C., 2009, *MNRAS*, 392, 135
- Lynden-Bell D., 1967, *MNRAS*, 136, 101
- Mahajan S., Mamon G. A., Raychaudhury S., 2011, *MNRAS*, 416, 2882
- Mahdavi A., Geller M. J., Böhringer H., Kurtz M. J., Ramella M., 1999, *ApJ*, 518, 69
- Maoz E., 1990, *ApJ*, 359, 257
- Menci N., Fusco-Femiano R., 1996, *ApJ*, 472, 46
- Mohr J. J., Geller M. J., Fabricant D. G., Wegner G., Thorstensen J., Richstone D. O., 1996, *ApJ*, 470, 724
- Natarajan P., Hjorth J., van Kampen E., 1997, *MNRAS*, 286, 329
- Owers M. S., Couch W. J., Nulsen P. E. J., 2009, *ApJ*, 693, 901
- Pimbblet K. A., Penny S. J., Davies R. L., 2014, *MNRAS*, 438, 3049
- Press W. H., Schechter P., 1974, *ApJ*, 187, 425
- Ribeiro A. L. B., Lopes P. A. A., Trevisan M., 2010, *MNRAS*, 409, L124
- Ribeiro A. L. B., Lopes P. A. A., Trevisan M., 2011, *MNRAS*, 413, L81
- Ribeiro A. L. B., de Carvalho R. R., Trevisan M., Capelato H. V., La Barbera F., Lopes P. A. A., Schilling A. C., 2013, *MNRAS*, 434, 784
- Rines K., Geller M. J., Kurtz M. J., Diaferio A., 2003, *AJ*, 126, 2152
- Rines K., Geller M. J., Kurtz M. J., Diaferio A., 2005, *AJ*, 130, 1482
- Rossetti M. et al., 2016, *MNRAS*, 457, 4515
- Ruckdeschel P., 2006, *Metrika*, 63, 295
- Solanes J. M., Manrique A., García-Gómez C., González-Casado G., Giovanelli R., Haynes M. P., 2001, *ApJ*, 548, 97
- Struble M. F., 1979, *AJ*, 84, 27
- van der Marel R. P., Magorrian J., Carlberg R. G., Yee H. K. C., Ellingson E., 2000, *AJ*, 119, 2038
- White S. D. M., 1996, in Lahav O., Terlevich E., Terlevich R. J., eds, *Gravitational Dynamics*. Cambridge Univ. Press, Cambridge, p. 121
- White S. D. M., Frenk C. S., 1991, *ApJ*, 379, 52
- Yahil A., Vidal N. V., 1977, *ApJ*, 214, 347
- Yang X., Mo H. J., van den Bosch F. C., Pasquali A., Li C., Barden M., 2007, *ApJ*, 671, 153
- York D. G. et al., 2000, *AJ*, 120, 1579
- Zhang Y.-Y., Andernach H., Caretta C. A., Reiprich T. H., Böhringer H., Puchwein E., Sijacki D., Girardi M., 2011, *A&A*, 526, A105

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