# Stellar Population Properties of ETGs in Compact Groups of Galaxies

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# **ABSTRACT**

We present results on the study of the stellar population in Early-Type galaxies (ETGs) belonging to 151 Compact Groups (CGs). We also selected a field sample composed of 846 ETGs to investigate environmental effects on galaxy evolution. We find that the dependences of mean stellar ages, [Z/H] and  $[\alpha/Fe]$  on central stellar velocity dispersion are similar, regardless where the ETG resides, CGs or field. When compared to the sample of centrals and satellites from the literature, we find that ETGs in GCs behave similarly to centrals, especially those embedded in low-mass haloes  $(M_h < 10^{12.5} M_{\odot})$ . Except for the low-mass limit, where field galaxies present a Starforming signature, not seen in CGs, the ionization agent of the gas in CG and field galaxies seem to be similar and due to hot, evolved low-mass stars. However, field ETGs present an excess of  $H\alpha$  emission relative to ETGs in CGs. Additionally, we performed a dynamical analysis, which shows that CGs present a bimodality in the group velocity dispersion distribution - a high and low- $\sigma$  mode. Our results indicate that high- $\sigma$  groups have a smaller fraction of spirals, shorter crossing times, and a more luminous population of galaxies than the low  $\sigma$  groups. It is important to emphasize that our findings point to a small environmental impact on galaxies located in CGs. The only evidence we find is the change in gas content, suggesting environmentally-driven gas loss.

**Key words:** galaxies: groups: general – galaxies: evolution – galaxies: stellar content – galaxies: interactions – galaxies: active

# 1 INTRODUCTION

Research in extragalactic astrophysics has made significant progress in the past fifteen years, mostly because of the large surveys that offered a deeper look into the Universe. Even with those undeniable advances, many open questions about the formation and evolution of galaxies still remain. We know that the environment plays a role in the evolution of galaxies, but the extension of that influence remains unclear, a good example of which are the associations of galaxies known as Compact Groups (CGs). They show high spatial density, despite being composed by no more than ten galaxies, and present a moderate velocity dispersion (~ 200 km/s), typical of galaxies in low density environments. Because of these properties, CGs are considered an ideal place for studying dynamical interactions and

mergers. They offer all conditions required for a merge to happen – high density and low relative velocities –, and early N-body simulations (Barnes 1985) estimated that after ~1 Gyr galaxies in CGs should merge into a "fossil" giant elliptical galaxy. Despite the fact that many groups show signs of mergers, the actual number of observed CGs is too high to fulfill such prediction. Later studies show that certain initial conditions (Di Matteo et al. 2008) or the dark matter distribution (Athanassoula, Makino & Bosma 1997) could prolong the lifetime of CGs for at least ~9 Gyr. Also, loose groups may be a source of replenishment for CGs (Diaferio et al. 1994; Governato, Tozzi & Cavaliere 1996; Ribeiro et al. 1998; Andernach & Coziol 2005; Mendel et al. 2011; Pompei & Iovino 2012). The fact that isolated CGs show an excess of Early-Type Galaxies (ETGs)

collaborates to such "replenishment mode" scenario (Andernach & Coziol 2007).

The type of gas ionization mechanism in CG galaxies may reflect these expected high merger rates and interactions. One way to trigger an AGN (Active Galactic Nucleus) is galaxy-galaxy interaction that may feed a supermassive black hole (SMBH) in the center of the galaxy. These interactions can also induce star formation if enough gas is involved in the process. In fact, ionization by AGN is conspicous in CGs, both in form of LINERs and low luminosity, high-ionization nuclear activity (Coziol et al. 1998; Coziol, Iovino & de Carvalho 2000; Martínez et al. 2008; Gallagher et al. 2008; Martínez et al. 2010). The deficiency of gas in these groups can explain the type of activity and the absence of new star formation episodes. Verdes-Montenegro et al. (2001) conclude, analyzing 72 systems defined by Hickson (1982), that CGs are ~ 40% depleted in HI from the expected value based on the optical luminosity and morphology of the member galaxies.

CGs are richer in elliptical galaxies than the field (Lee 2004; Deng, He & Wu 2008). Galaxies in CGs also tend to be older than galaxies in the field (Proctor et al. 2004; de La Rosa et al. 2007; Plauchu-Frayn et al. 2012) but have similar ages when compared to clusters (Proctor et al. 2004). This is often interpreted as an indication that CGs speed up the evolution of galaxies from star forming to quiescent (Tzanavaris et al. 2010; Walker et al. 2010; Coenda, Muriel & Martínez 2012). Some authors even find evidence of truncation in the star formation for galaxies in CGs (de La Rosa et al. 2007). All these observations reinforce the scenario where CGs are gas-poor systems.

In this work, we investigate the stellar population properties of ETGs in CGs and their relation to the dynamics of these groups and gas ionization source present in these galaxies. For a better understanding of the effects caused by the CG environment, we compare our results to those obtained for a sample of ETGs in the field (low density) and to those determined for a sample of central galaxies studied by La Barbera et al. (2014).

This paper is organized as follows. In Section 2, we describe the samples in different environments and how we discriminate galaxies of different morphologies. Section 3 presents the methods applied to estimate the stellar population parameters. An analysis of the gas ionization agent in our sample is discussed in Section 4, followed by a dynamical analysis of our sample of CGs in Section 5. We discuss our results and present a summary in Section 6.

# 2 SAMPLE AND DATA

The focus of this study is the ETGs belonging to CGs. For the definition of the sample, we choose the extensive catalogue of bright galaxies in CGs defined by McConnachie et el. (2009). After the selection, we performed a visual classification to select the elliptical galaxies belonging to CGs. For this, we mimic the same scheme applied in the second version of "The Galaxy Zoo Project" (Willett et al. 2013). We also defined a control sample, constituted of ETGs in the low-density environment (field), as we discuss below.

## 2.1 The Compact Group Sample

Our sample of CGs was extracted from the "Catalogue A" compiled by McConnachie et el. (2009). This catalogue includes objects classified as galaxies and with magnitude in the r band brighter than  $m_r = 18$  in the database of the sixth release of the Sloan Sky

Table 1. Summary of the number of group members with spectra available in SDSS DR12. We list the number of groups,  $N_{groups}$ , with  $N_z$  members with redshifts available and the total number of members,  $N_{members}$ .

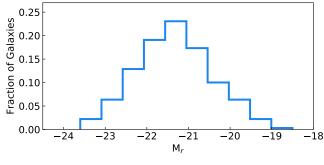
81
81
30
10
5
3
13
6
1
1
1

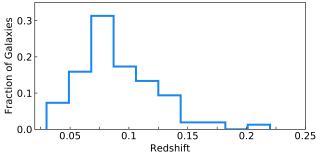
Digital Survey (SDSS DR6). Compact groups were identified using the three well-known photometric criteria determined by Hickson (1982). The first criterion, population, specifies that CGs must be composed by at least four members in the magnitude range  $[m_1, m_1 + 3]$ , where  $m_1$  is the magnitude of the brightest group member. The compactness criterion states that the group mean surface brightness,  $\langle \mu_e \rangle$ , must be brighter than 26 mag/arcsec<sup>2</sup> in the r-band. The last one, the isolation, establishes that no objects in the same magnitude range as the CG member galaxies are present in a ring of angular size  $\theta_G \geqslant 3\theta_N$ , where  $\theta_N$  is the smallest concentric circle encompassing the centre of the galaxies defining the group. Taking all these criteria into account, the catalogue ends up with 2297 CGs (9713 galaxies) covering the magnitude range  $14.4 \leqslant r \leqslant 18.0$  and redshift  $z \leqslant 0.2$ . By visual inspection of the objects in Catalogue A, the authors eliminate the contamination by photometric errors from the SDSS algorithm, such as misclassified objects, satellite tracers and saturated objects. However, when considering the spectroscopic data, the authors estimate that 55% of the CGs present interlopers.

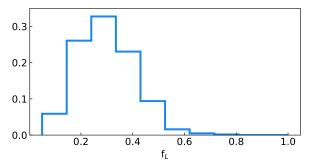
To increase the spectroscopic data available, we have searched for the galaxies from Catalog A in the database of the twelfth release of SDSS (DR12) (Alam et al. 2015). We found that the spectra of ~ 53% (5353 galaxies) of the objects in Catalog A are available in DR12. From that initial sample, we selected only groups with at least 4 members with redshifts satisfying the concordant redshift criterion ( $\Delta cz \leq 1000$  km/s) as in Hickson et al. (1992). We do not include a colour criterion given the well-know degeneracy with the age and metallicity which are parameters that we are interested in investigating. Our final sample of CGs is composed by 629 galaxies distributed in 151 GCs. Some galaxy properties such as absolute magnitude  $M_r$ , redshift and fraction of light captured by the optical fiber  $(f_L)$  are presented in Figure 1. Table 1 summarizes, for the whole sample, the number of groups  $N_{groups}$ , with  $N_z$  members with redshift available and the total number of members,  $N_{members}$ .

# 2.2 Morphology for the CG Sample

For the morphological selection, we apply the same methodology used in The Galaxy Zoo Project (Lintott et al. 2011; Willett et al. 2013). This project, after more than a decade of existence, has produced four catalogues of galaxy morphological classifications. We searched, in the first and second versions of the catalogue, the morphological classification for the 629 galaxies that compose our







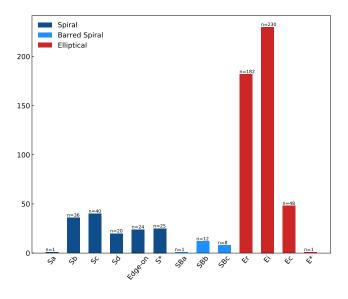
**Figure 1.** Absolute magnitude  $(M_r)$ , redshift and fraction of light  $(f_l)$  distributions for the 629 galaxies that composed our sample of GCs. The parameter  $f_l$  is defined as the fraction of light captured by the SDSS fiber aperture.

sample. From the first catalogue (hereafter "Zoo1"), around 70% (441) of the galaxies in our sample have morphology determined, although 309 out of those 441 systems are listed as "Unknown". For the second version of the catalogue (hereafter "Zoo 2"), more restrictions were applied for the selection of the objects in terms of size (petroR90 $_r$  > 3 arcsec, where petroR90 $_r$  is the parameter that measures the radius containing 90% of the Petrosian flux in the r band), brightness (Petrosian half-light magnitude  $m_r$  <17.0) and redshift (0.0005 < z < 0.25). Since Zoo 2 presents morphological classifications for only the brighter galaxies in SDSS DR7, the number of objects from our sample found in the catalogue was correspondingly low (only 331), with most of them classified as ellipticals ( $\sim$  54%).

The lack of morphological classifications for low-brightness galaxies, led us to reproduce the same form and use the decision tree from Zoo 2 and apply to the galaxies of our sample. A total of five persons responded to the questionnaire, and the most voted answers determined the class attributed for each object. Table 2 presents a list of the classification categories and Figure 2 shows a summary for all the 629 galaxies from our sample. A brief explanation of each category from Zoo 2 is given in Table A1 in the Appendix.

**Table 2.** The morphological classification of the galaxies belonging to our MC09 sample. The table contains 629 lines but only the first 10 objects are reproduced here. We adopted the same nomenclature from The Galaxy Zoo 2 Project, where the letter inside parenthesis means: (m) = merger, (l) = lens/arc, (r) = rings, d = disturbed, i = irregular, (o) = others and (d) = dust lane. The "GroupID" is the number of the group given in McConnachie et el. (2009), "GalID" is the position of the galaxy in order of brightness in the group and "ObjID" is the identification of the object in SDSS DR12 database. The full table is available online.

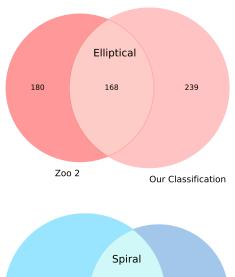
GroupID	GalID	ObjID	Class
42	1	1237661137960632449	Er
42	3	1237661137960632448	Ei
42	4	1237661137960632447	Ei
42	2	1237661137960632446	Ei
46	4	1237654390032629949	Er
46	3	1237654390032629946	Ei
46	2	1237654390032629944	Ei
46	1	1237654390032629943	Er
70	4	1237662224058024106	Ei
70	2	1237662224058024105	Ei(m)

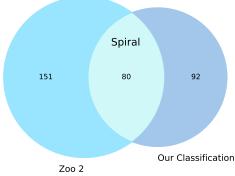


**Figure 2.** Distribution of galaxies according to the morphological classification performed by five voters for the galaxies in our CG sample.

Our rating leads to a sample composed mostly by elliptical galaxies ( $\sim 84\%$ ). For one elliptical galaxy, the voters did not specify the shape, and for 25 spirals there is no information about the presence of the bulge. In this last case, the galaxy is listed as "S".

To estimate how reliable our classification is, we compare our result for those 331 galaxies in common with the Zoo 2 database, as shown in Figure 3. According to Zoo 2, 180 galaxies among those 331 systems are ellipticals. Our classification is in agreement for 168 from those 180 elliptical galaxies (superior panel of Figure 3). Considering the completeness as the fraction of galaxies with the same class in both classification schemes, we estimated a completeness of  $\sim 93\%$ . For estimating the contamination in our classification, we count the number of spirals given in Zoo 2 catalogue (151 galaxies) which are classified as ellipticals in our experiment (71 galaxies), as shown in the inferior panel in Figure 3. This leads to contamination rate of  $\sim 51\%$ . This high contamination could be the reflex of the





**Figure 3.** Comparison between the classifications of 331 galaxies of our sample that also belong to the Galaxy Zoo 2 catalogue. We apply the same methodology of the second version of the project to perform our morphological classifications.

low number of voters in our classification compared with the thousands of voters from Zoo 2; however, all voters in our experiment are experienced astronomers. Our final sample of ellipticals in CGs are those 461 galaxies classified as such by our voters.

# 2.2.1 Field ETGs Sample

In order to perform a consistent analysis of the effects of the environment on galaxies in GCs, we have selected a control sample of elliptical galaxies in the low density environment of the field. This allow a rich comparison between the properties of these galaxies in different environments. For the field galaxy sample we selected only galaxies that are more distant than 10  $R_{vir}$  from all groups with halo masses greater than  $10^{13} M_{\odot}$ , following the approach described in Trevisan et al. (2017). We used the updated version of the group catalog compiled by Yang et al. (2007). This updated catalogue contains 473 482 groups drawn from a sample of galaxies mostly from the SDSS-DR7 (Abazajian et al. 2009). Although the catalogue by Yang et al. (2007) contains objects up to  $z \leq 0.2$ , we cut our sample in z = 0.14, since the catalogue is complete for groups with halo masses  $\gtrsim 10^{13}\,\mathrm{M}_\odot$  below this redshift (see Figs. 5 and 6 in Yang et al. 2007). To be consistent, we applied the same redshift cut to the ETGs in CGs, leading to a sample with 423 CG galaxies used for the matching procedure. The initial field sample is then composed by 130767 galaxies. We then selected only the galaxies that are classified as elliptical according to the Galaxy Zoo 2, reducing the sample to 17 499 galaxies. To assure that the galaxy

is not close to a group or cluster outside the borders of the SDSS, we require that at least 95 per cent of the region within 500 kpc from the galaxy lies within the SDSS coverage area. For this purpose, we adopted the SDSS-DR7 spectroscopic angular selection function mask provided by the NYU Value-Added Galaxy Catalog team (Blanton et al. 2005) and assembled with the package MAN-GLE 2.1 (Hamilton & Tegmark 2004; Swanson et al. 2008). We excluded 3179 galaxies that do not satisfy this criterion. Finally, we extracted from this sample of 14 320 objects a control sample of 846 galaxies (twice the size of the GC sample) with similar stellar masses, at similar redshifts and with similar fraction of light within the SDSS fiber as the CG sample by applying the Propensity Score Matching (PSM) technique (Rosenbaum & Rubin 1983). For the PSM, we used the MatchIt package (Ho et al. 2011) written in R (R Core Team 2015). This technique allows us to select from the sample of field galaxies a control sample in which the distribution of observed properties is as similar as possible to that of the CG galaxies. We adopted the Mahalanobis metric (Mahalanobis 1936) and the nearest-neighbour method to perform the matching. In Figure 4 we compared the distribution in  $M_r$ , redshift and  $f_L$  for both samples used in this work. We also executed a permutation test in order to check if the distributions are indeed similar. The p-value for the distribution of absolute magnitude (p = 0.45), redshift (p = 0.13) and the fraction of light within the SDSS fiber (p = 0.16) allows to reject the null hypothesis and consider that the samples came from the same parent population.

# 3 STELLAR POPULATION PARAMETERS

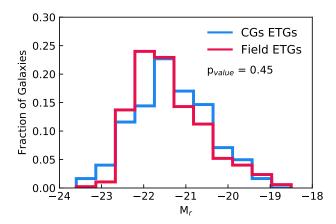
A way to characterize a stellar population is determining quantities like mean stellar age, metallicity, [Z/H], and alpha enhancement,  $[\alpha/\text{Fe}]$ . There are two widely used techniques to recover those parameters: spectral fitting and spectral index analysis. In the following, we describe how we combined both techniques to estimate all relevant stellar population parameters for our samples of ETGs.

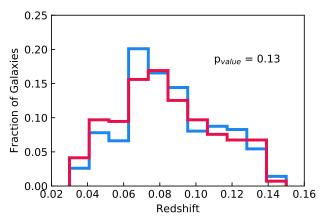
For better results, we limited our sample to galaxies which spectra provide a signal to noise ratio of  $S/N \geqslant 15$  and velocity dispersion between  $70 \leqslant \sigma_0 \leqslant 420$  km/s. This final cut leads to a sample of 303 ETGs in CGs and 697 in the field. In the next section, we compare the results for these samples.

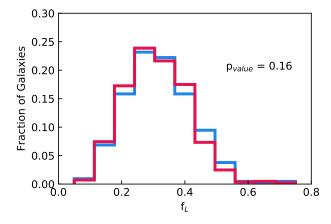
# 3.1 Spectral Fitting

For our spectral-fitting methodology, we consider that a galaxy spectrum can be represented as a linear combination of a set of Single Stellar Populations (SSPs). We use a set of 108 SSPs extracted from the extended MILES (MIUSCAT) library (Vazdekis et al. 2010) covering stellar populations with 27 ages between 0.5 and 17.78 Gyr and four metallicities –  $[M/H] = \{-0.71, -0.40, 0, 0.22\}$ . These models use the Padova isochrones and a Kroupa Universal Initial Mass Function. The SSPs cover the wavelength interval from 3465 to 9469 Å with a spectral resolution of ~2.51 Å (FWHM). This is the same set used in the SPIDER Project (La Barbera et al. 2014).

The full spectral fitting is performed with the STARLIGHT code (Cid Fernandes et al. 2005; Mateus et al. 2007; Asari et al. 2007). Before running the code, the observed spectra are corrected for foreground Galactic extinction and shifted to the rest frame. As for the models, we degraded the spectra to the mean resolution of SDSS (3 Å). We performed the fitting in the wavelength interval of 4000 - 5700 Å, which excludes the blue regions where the abundance ratio of non-solar elements could lead to a bias when we use nearly







**Figure 4.** Comparison between the distributions of redshift, k-corrected absolute magnitude in the r band  $(M_r)$  and the fraction of light  $(f_L)$  for the field and CGS samples. The p-value was estimated through a permutation test

solar SSPs (Miles). This interval also excludes the regions with presence of molecular bands such as TiO that cannot be well-fitted with solar-scale models and a Kroupa IMF (La Barbera et al. 2013). As for the extinction law, we select the more appropriate for elliptical galaxies, given by Cardelli, Clayton & Mathis (1989). The program output gives the "population vector"  $(x_j)$ , which is the fraction of the total light that each SSP contributes to the fitting. From the

spectral fitting, we derive the mean stellar age as a function of  $x_j$  through

$$< \log t_* > = \sum_{j=1}^{N_*} x_j \log t_j / \sum_{j=1}^{N_*} x_j,$$
 (1)

where  $t_i$  is the age of the *j*th SSP.

#### 3.2 Spectral Index

To complete the set of stellar population parameters, we use the spectral index technique to estimate the stellar metallicities and  $[\alpha/\text{Fe}]$ . We measure the line strengths of the lines Fe5270, Fe5335, Fe4383 and Mg $_b$ 5177 using the code indexf (Cardiel (2010)). From the iron indices, we estimated the  $\langle Fe_3 \rangle^1$ , an index sensible to [Z/H]. We also use the [MgFe]' index as defined by Thomas, Maraston & Bender (2003) ( $[MgFe]' = \{Mgb[0.72(Fe5270) + 0.28(Fe5335)]\}^{1/2}$ ) for estimation of the  $[\alpha/\text{Fe}]$  parameter.

To remove the effect of the velocity dispersion we applied the broadening correction to the spectral index as defined in de La Rosa et al. (2007). The correction is the ratio between the index measured with a given velocity dispersion and the one measured in the rest frame ( $\sigma$  = 0). The ratios are determined using the indices measured from the spectra produced using the model from Vazdekis et al. (2010) customised for a set of velocity dispersions (50 - 350 km/s). Our correction is in excellent agreement with those applied by de La Rosa et al. (2007), which use the models from Vazdekis (1999).

#### 3.3 Alpha enhancement

In the study of stellar populations, the  $[\alpha/\text{Fe}]$  parameter holds valuable information about the formation and evolution of the galaxy. The Fe and  $\alpha$ -element abundances relevant for the  $[\alpha/\text{Fe}]$  parameter are products of the final stages of the evolution of massive stars, where Fe comes mainly from the type Ia supernova while  $\alpha$ -elements are produced by core-collapse Supernovae explosions. Stellar populations are formed from the gas present in Intergalactic Medium (IGM) and this medium is enriched in metals by supernova explosions or stellar winds. In this sense, by recovering their relative abundances of stellar populations we are also tracing their formation history.

The estimation of  $[\alpha/Fe]$  was made through a solar scaled proxy. The proxy is defined as the difference between two independent metallicities:  $[Z_{Mgb}/Z_{Fe}] \equiv [Z/H]_{Mgb} - [Z/H]_{Fe}$ . The metallicities are calculated fixing the age coming from the spectral fitting and by a polynomial fit with the metallicities and the indices  $Fe_3$  and  $Mg_b$  from the MILES models (Vazdekis et al. 2010). Finally, for the  $[\alpha/Fe]$  we use the relation defined in La Barbera et al. (2013):  $[\alpha/Fe] = 0.55[Z_{Mgb}/Z_{Fe}]$ .

#### 3.4 Hybrid Method

The result from the hybrid method is a combination of the age obtained from the spectral fitting and the parameters [Z/H] and  $[\alpha/Fe]$  estimated from the spectral index method. The [Z/H] value is calculated using the approach described for the  $Z_{Fe}$  and  $Z_{Mg}$ , but now we perform a polynomial fit using the metallicity and [MgFe]'

<sup>&</sup>lt;sup>1</sup>  $\langle Fe_3 \rangle \equiv \frac{1}{3} (Fe_{5270} + Fe_{5335} + Fe_{4383})$ 

index from the MILES models. The  $[\alpha/\text{Fe}]$  parameter is estimated as described in Section 3.3.

In Figure 5, we present the stellar population parameters as a function of the central velocity dispersion for ETGs in CGs (blue dots) and field (red dots). Since the central velocity dispersion depends on the distance and the aperture size of the optical fibre, it is necessary to apply an aperture correction. We use the correction given as a power law by Jorgensen et al. (1995),  $\log(\sigma_{ap}/\sigma_n) = -0.04 \log(r_{ap}/r_n)$ , where  $\sigma_{ap}$  is the velocity dispersion from SDSS DR12 measured through an aperture  $r_{ap} = 1.5'$  for the spectrograph used in the Legacy SDSS program or  $r_{ap} = 1.0'$  for the objects observed in the BOSS program. We set  $r_n = 1/8r_e$ , where  $r_e$  is the effective radius; in this case, we use the de Vaucouleurs radius given by the deVRad<sub>r</sub> parameter from the DR12 SDSS database. A wrong sky subtraction or weak spectral lines could compromise the index measure providing unrealistic  $[\alpha/Fe]$  in the final application of the hybrid method. Because of such errors, a total of 30 galaxies from the field sample are not included in our results. From the CGs sample, only one ETG was excluded for the same reason.

Our result show that the stellar populations present in ETGs belonging to CGs behave similarly as the ETGs in the field. The stellar population parameters from both samples increases towards systems with higher central velocity dispersion. Once the velocity dispersion is an indirect measure of the dynamical mass of the system, our results show that massive galaxies are older, more metalrich and with higher  $[\alpha/Fe]$  than the less massive (low- $\sigma$ ) ETGs. The only noticeable difference is for the age in the low- $\sigma$  regime ( $\sigma \leqslant \sim 130$  km/s), where the ETGs in CGs seems to be older ( $\sim 2$  Gyr) than the ones in the field.

# 4 ACTIVITY ANALYSIS

Following the purpose of establishing differences between ETGs in the environments of CGs and field, we also analysed the type of ionization sources responsible for the emission lines in our sample. For such, we measured relevant emission lines fluxes and equivalent widths after stacking our individual spectra to increase the signal-to-noise ratio, and used diagnostic diagrams to perform the classification, as we describe below.

# 4.1 Stacked Spectra

Optical diagnostic diagrams rely on emission line ratios, which are prone to significant uncertainties if the individual line fluxes are not well constrained. Those diagrams also require spectra with a high signal-to-noise ratio to minimise errors in the calculation of line ratios. It could be even more challenging if we are dealing with galaxies presenting weak emission lines, such as ellipticals. The spectra of our ETGs samples present typical S/N values in the order of ~20; because of this, for the gas ionization source analysis, we have used stacked spectra. Stacking spectra allows for an increase in the S/N ratio, which leads to a more reliable result. The stacked spectra were produced by median-combining the individual normalized spectra in bins of velocity dispersion between  $\sigma = 70 - 300$  km/s. The bin widths were determined in a way that each bin has a certain minimal number of galaxies. For the sample of ETGs in CGs we defined a minimum of  $N_{bin} \geqslant 20$ galaxies per bin, and for the field sample, we used  $N_{bin} \ge 60$ . In this way, the width of the bins varies from 10 to 50 km/s. Our analysis is based on eleven spectra for the CGs sample and eight from the field

#### 4.2 Diagnostic Diagrams

We have used the diagnostic diagrams defined by Baldwin, Phillips & Terlevich (1981) and Cid Fernandes et al. (2011) to classify the type of activity in our ETG samples. In order to correct the emission features for stellar absorption, we have subtracted from the stacked spectra the corresponding best-fit stellar population synthesis solution obtained with STARLIGHT. The fits described in Sect. 3.1 are not suitable for this purpose, since they do not extend to some important optical transitions above 6000Å (e.g. the H $\alpha$  line). We have therefore performed a new run of STARLIGHT similar to the previous one, but extending the fitting window to 6900Å. After subtraction of the best-fitting models, the emission line fluxes of  $H\beta$ , [OIII] $\lambda$ 5007, [NII] $\lambda$ 6548, H $\alpha$  and [NII] $\lambda$ 6584 were measured by Gaussian fitting the relevant spectral ranges in each stacked spectrum. This fit was done taking into account the uncertainties in all spectral pixels and the wavelength-dependent resolution of the SDSS spectra. The continuum around each line was allowed for a constant tilt, to account for possible mismatches between SSP models and the stacked spectra. The H $\beta$  and [OIII] $\lambda$ 5007 have been fitted individually, but a simultaneous fit was applied to the triplet [NII] $\lambda$ 6548-H $\alpha$ -[NII] $\lambda$ 6584. Line equivalent widths have been obtained as the ratio between the line fluxes and the median continuum at the central wavelength of the emission lines, measured directly on the best-fit STARLIGHT spectrum. An example of the emission line fitting is shown in Figure 6.

For the BPT diagram (Baldwin, Phillips & Terlevich 1981), we use the AGN, Star Forming and Transition (Composite) separation lines defined in Kewley et al. (2001) and Kauffmann et al. (2003) and the limits set in Kewley et al. (2006) to separate Seyferts and LINERs. In Figure 7, we show the BPT diagrams for the stacked spectra from the CGs and the field sample. The colours of the points indicates the galaxy velocity dispersion ( $\sigma$ ), from dark blue (low- $\sigma$ ) to dark red (high- $\sigma$ ). The stacked spectra of ETGs in CGs is spread between the LINERs and Transition regions with the highest  $\sigma$  stacks concentrated in the LINERs partition. For the field sample, two of the lowest- $\sigma$  stacks resides outside the "LINERs" part of the diagram where the other stacks are located. The stack with  $70 \leqslant \sigma < 100$  km/s is classified as "Starforming" and the stack with  $100 \leqslant \sigma < 130$  km/s is classified as a "Transition" object.

The BPT diagram, albeit a good diagnostic regarding the ionization source for galaxies with strong emission lines, is not able to discriminate between genuine, AGN induced LINER-like emission and other ionization mechanisms unrelated to accretion by a supermassive black hole. The WHAN diagram, on the other hand, supplies a classification scheme for weak emission line galaxies whose classification is ambiguous, separating true LINERs from spectra whose emission lines are due to ionization by hot, evolved low-mass stars (HOLMES) – i.e. "retired" objects, with no star formation whatsoever. The WHAN diagram therefore discriminates galaxies in five classes of gas ionization mechanisms using the following criteria:

- (i) pure star-forming galaxies: log[NII]/H $\alpha$  < -0.4 and  $W_{\mbox{H}\alpha}$  > 3 Å
  - (ii) Seyferts:  $\log[N \text{ II}]/H\alpha > -0.4$  and  $W_{H\alpha} > 6 \text{ Å}$
  - (iii) LINERs:  $\log[N \text{ II}]/H\alpha > -0.4$  and  $3 < W_{H\alpha} < 6 \text{ Å}$
  - (iv) Retired galaxies:  $W_{\text{H}\alpha}$  < 3 Å
  - (v) Passive galaxies:  $W_{\text{H}\alpha}$  and  $W_{\text{[N II]}} < 0.5 \,\text{Å}$

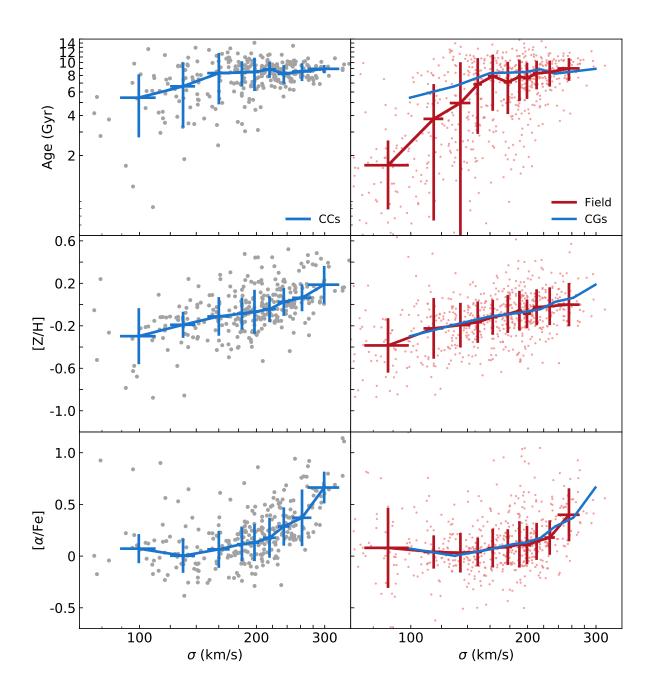


Figure 5. Stellar population parameters obtained from the application of the hybrid method. On the left panels, we show the mean stellar age, [Z/H] and  $[\alpha/Fe]$  trends for the 302 ETGs in CGs. In the right panels we compare the trends for the field sample (682 galaxies – in red) and the CGs sample. The age is estimated from the spectral fitting and the [Z/H] and  $[\alpha/Fe]$  are calculated using a proxy. The [Z/H] proxy is given from the polynomial fitting of the metallicity and values of the [MgFe]' from the MILES models (Vazdekis et al. 2010). The  $[\alpha/Fe]$  is calculated using the relation from La Barbera et al. (2013).

In Figure 8 we present the WHAN diagram for the stacked spectra from both samples. The stack spectra of ETGs in CGs with the highest  $\sigma$  falls in the "Passive" region of the diagram while other stacks are mostly concentrated in the bottom part of the "Retired" area. The field sample is majority located in the "Retired" part of the diagram, with the lowest- $\sigma$  bins being closed to the LINERs area and the highest- $\sigma$  spectra are in the bottom of the "Passive" region. The exception is the two lowest  $\sigma$  bins that is classified as Starfoming and LINERs. Notice, however, that the WHAN diagram

presents a less defined frontier between Starforming and Seyfert-like spectra, so we can confidently confirm that the source of gas ionization is associated to young massive stars.

Considering that our sample is composed of ETGs, the absence of active star formation as indicated by the BPT and WHAN diagrams is not a surprise. However, star formation (Patton et al. 2013) or AGN activity (Silverman et al. 2011) can be induced by galaxy interactions, resulting in an increase of AGN or SF optical signatures. The diagnostic diagrams have shown that the ionization

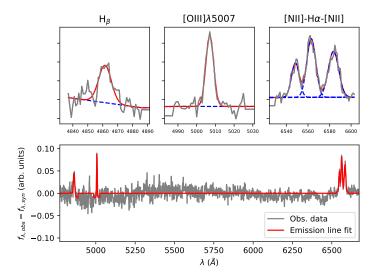
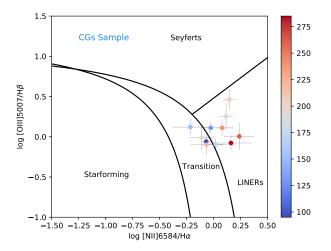


Figure 6. An example of the Gaussian fitting used to measure the fluxes of the emission lines in the stack spectra. The top panels show the individual fitting of the H $\beta$  and [OIII] $\lambda$ 5007 lines and the simultaneous fitting for the triplet [NII] $\lambda$ 6548-H $\alpha$ -[NII]. In the bottom panel, we exhibit the full spectra and the detected emission lines.



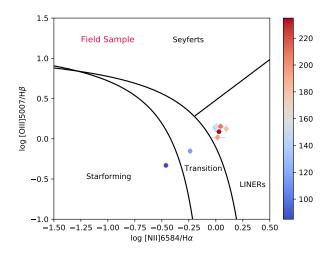


Figure 7. The BPT diagram for the stacked spectra from the sample of ETGs in GCs (left) and in the field (right). The color scale is based on the velocity dispersion of the stack from blue to red as the velocity dispersion increases.

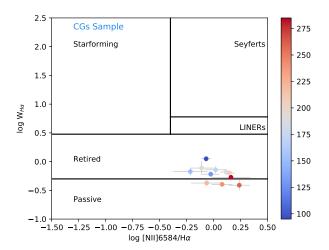
source is similar for ETGs in CGs or in the field, with no detectable contribution of ongoing star formation or ionization by a supermassive black hole in almost all bins. Therefore, the ionization field of the ETGs in our sample seems to present a small sensitivity to the environment. However, Figure 8 also reveals a shift in the equivalent width of H $\alpha$  of field galaxies with relation to galaxies in CGs: even though the ionization agent does not vary significantly, the line emission is more intense in field galaxies. This hints at a reduction of the total ionizable gas budget in CG galaxies as compared to their field counterparts.

We have checked the robustness of our gas ionization source characterization scheme against stack contamination by galaxies containing strong emission lines. We have performed a visual analysis of individual spectra in a given stack in order to identify such objects. We have found a low ( $\sim 9-13\%$ ) level of contribution by strong line emitters. Excluding these objects from the stacks, the re-

sulting equivalent widths of  ${\rm H}\alpha$  are reduced by 2-4%. This variation is much lower than the typical differences between stacks and barely affects the position of a stack in the WHAN diagram. This very low sensitivity to outliers is due to our choice of median-combining rather than average-combining individual spectra. Our results are therefore not affected at all by objects with intense emission lines.

# 5 DYNAMICAL ANALYSIS

We investigate the dynamics of the CGs in our sample by performing an analysis of the velocity dispersion distribution using the MCLUST package for model-based clustering. MCLUST is an efficient R package for modeling data as a Gaussian finite mixture (Fraley & Raftery 2002). A basic explanation of how MCLUST works is presented in de Carvalho et al. (2017). In the present anal-



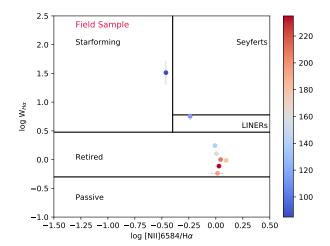
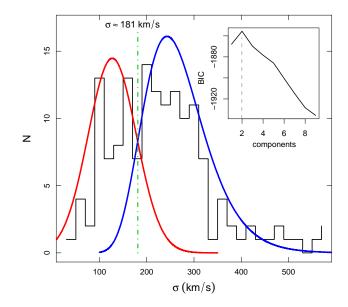


Figure 8. WHAN diagram for the stacked spectra from the sample ETGs in GCs (left) and in the field (right). The color scale is identical to Figure 7.

ysis, we initially ran the code for a Gaussian mixture model and found two modes in 97% of the times out of 1000 re-samplings. This methodology shows the robustness of the finding. However, while MCLUST indicates bimodality in the data, the Gaussian mixture is not necessarily the best fit for the distribution. Taking this into account, we compare three specific mixtures: normal-normal, normal-lognormal, and normal-gamma distributions. We find the normal-lognormal mixture to be the best model from the likelihood ratio. Adopting this model, we divide our sample into two classes following the distribution of the velocity dispersion of the group  $(\sigma_G)$ : low  $\sigma$  groups  $(\sigma_G \leqslant 181 \text{ km/s})$  and high  $\sigma$  groups  $(\sigma_G > 181 \text{ km/s})$  as is shown in Figure 9. The fraction of groups, from the total of 151 CGs, that falls in each regime is given in Figure 10.

The high and low  $\sigma$  groups exhibit different absolute magnitude distributions (total luminosity of all galaxies in a given group) as we can see in Figure 11. The permutation test<sup>2</sup> takes all possible combinations of group membership and creates a permutation distribution from which one can assess evidence that the two samples come from two different populations. The test gives a p-value of 0.004 implying rejection of the null hypothesis that the two distributions come from the same parent population. Groups in the high- $\sigma$  regime have more luminous galaxies than the low- $\sigma$  groups with magnitudes extending to  $M_r = -25$  mag.

The two groups also distinguish themselves wrt the predominant morphological types. In Figure 12 we show the distribution of the spiral fraction for low and high- $\sigma$  groups where we can clearly see how different the distributions are, confirmed by the p-value estimated using the Proportional Test<sup>3</sup> (p-value of 0.03), for testing how probable it is that both proportions are the same. The fraction of groups with low spiral fraction (<0.3), namely dominated by early-type systems, is larger for high- $\sigma$  groups - more massive groups tend to have more early-type systems. On the other hand, examining the fraction of groups with high spiral fraction (>0.3), we conclude that less massive groups are dominated by late-type



**Figure 9.** The result from 1000 re-samplings and the fitting of a normal (red) and normal-lognormal (blue) in the mixture model. The CGs of our sample is divided into two groups concerning the velocity dispersion: low  $\sigma$  groups with  $\sigma_G \leq 181$  km/s and high  $\sigma$  groups with  $\sigma_G > 181$  km/s for  $\sigma_G$  as the velocity dispersion of the group. We also show the Bayesian Information Criterion (BIC) that indicates that the distribution of velocity dispersion of the groups has two components.

galaxies. In Figure 13, we exhibit the fraction of spirals versus group velocity dispersion relation where again the clear correlation (spiral fraction decreases with group velocity dispersion) is noticeable. We note that the last bin (higher velocity dispersion) shows an increase in spiral fraction, result also obtained by Ribeiro et al. (1998). We also show in Figure 13 the result from Ribeiro et al. (1998) in the study of dynamical properties of 17 HCGs. In Ribeiro et al. (1998)

<sup>&</sup>lt;sup>2</sup> Using the function permTS in R package under the library perm Fay (2009)

<sup>&</sup>lt;sup>3</sup> Using the function *prop.test* in R package

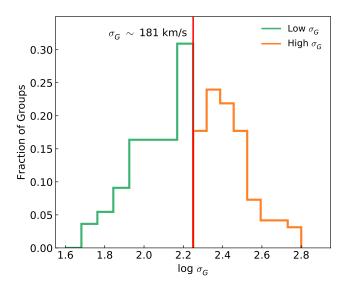


Figure 10. Distribution of the 151 CGs of our sample in term of group velocity dispersion ( $\sigma_G$ ). The groups are separated into two families: low- $\sigma$  and high- $\sigma$ . The low- $\sigma$  groups have  $\sigma_G <$  181 km/s. The red dashed line is the threshold limit that separates the two groups.

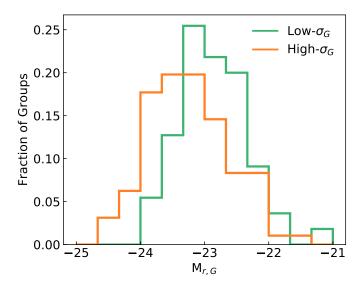


Figure 11. The distribution in  $M_r$  for the low and high  $\sigma$  groups of our sample of CGs. The p-value calculated from the Permutation Test (p = 0.004) indicates that the distributions came from different parent populations.

the morphological classification is based on the equivalent width of the H $\alpha$  spectral line (EW(H $\alpha$ ) > 6 is considered a late-type) which explains the slightly higher spiral fraction when compared to ours. Nevertheless, both trends are quite in agreement.

An additional parameter revealing the CGs dynamics is the crossing time, defined as the time for a galaxy transverse the group. Its simple version can be written like:

$$t_c = \frac{4}{\pi} \frac{R}{V} \tag{2}$$

where R is median of the two-dimensional galaxy-galaxy separation vector and V is the three-dimensional velocity dispersion estimated as  $V = [3(\langle v^2 \rangle - \langle v \rangle^2 - \langle \delta v^2 \rangle)]^{1/2}$ , with v being the radial velocity of

the galaxies of the group,  $\delta v$  the velocity error and the bracket means the average over all galaxies in the group. From the distribution of the crossing time for low- and high- $\sigma$  groups, shown in Figure 14, we can clearly see that low  $\sigma$  groups have higher crossing times.

It is expected that groups with a small crossing time will suffer more galaxy-galaxy interactions. Since such interactions are responsible for transforming the morphology of a galaxy, from late-type to early type, it is reasonable to expect that groups with smaller crossing times show a lower fraction of late-type galaxies. In Figure 15 we show the fraction of spirals as a function of the crossing time for 151 CGs in our sample. The points represent the mean of the crossing time of at least 11 groups in each bin and the error bar is the  $1-\sigma$  error. We found the same correlation as Hickson et al.

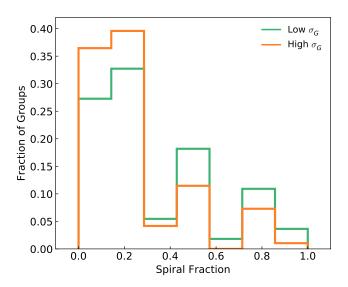


Figure 12. The spiral fraction distribution for low and high  $\sigma$  groups of our CGs sample. The p-value estimated from the Proportion Test (p = 0.03) confirms that the two distributions are distinct.

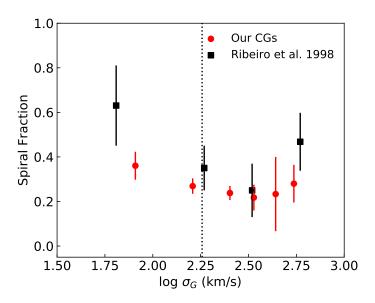


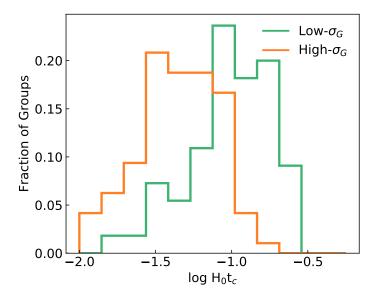
Figure 13. The spiral fraction against the velocity dispersion for CGs of our sample (red dot). The traced line separates the two velocity dispersion groups. We also show the results from the study by Ribeiro et al. (1998) with 17 CGs (black square).

(1992) and Ribeiro et al. (1998): the spiral fraction is is lower for groups with small crossing time.

Another important aspect of the study of CGs is to understand how their dynamical properties are linked to the stellar population properties of the member galaxies. In Table A2 we list the dynamical parameters for all the 151 CGs in our sample. The parameters are: (1) the identification of each group; (2) number of members in each group; (3) total absolute magnitude of the group in the r-band,  $M_{r,G}$ ; (4) velocity dispersion of the group; (5) harmonic radius (Mpc); (6) total dynamical mass (in  $M_{\odot}$ ); (7) the crossing time (in  $H_0^{-1}$ ); (8) spatial density; (9) spiral fraction; and (10) dynamical class, either low- $\sigma$  (L) or high- $\sigma$  (H). In Figure 16, we present

the distributions of Age, [Z/H], and [ $\alpha$ /Fe] for ETGS belonging to low and high- $\sigma$  groups. Additionally, we estimate the mean value of each distribution for the parameters: Age(L, H)= (7.82, 8.07) Gyr; [Z/H](L, H)= (-0.07, -0.01); and [ $\alpha$ /Fe](L, H)= (0.16, 0.28). Although the mean values are close, between low and high- $\sigma$  distributions, the Permutation Test indicates that the [Z/H] and [ $\alpha$ /Fe] parameters have different distributions in low- and high- $\sigma$  CGs, with p-values equal to 0.027 and 0.001, respectively. On the other hand, the age distribution for high and low- $\sigma$  groups are almost indistinguishable as is clear from the median values and the p-value = 0.341.

Looking at the distributions and mean values of the age,  $[\mathrm{Z/Fe}]$ ,



**Figure 14.** The distribution of the crossing time for low and high- $\sigma$  groups of our sample.

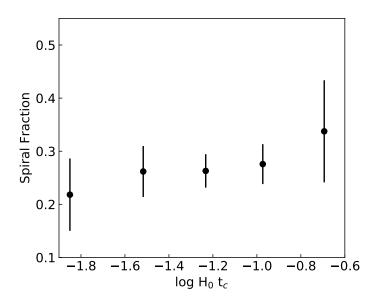


Figure 15. The fraction of spiral as a function of the crossing time for the 151 CGs of our sample. The points are given by the mean in each bin and the error bar is the 1- $\sigma$  error.

and  $[\alpha/\text{Fe}]$  of Figure 16, it can be noted that the ETGs belonging to the high- $\sigma$  CGs are formed slightly earlier and faster than the low- $\sigma$  CGs. The age difference in the mean values between the high- $\sigma$  and low- $\sigma$  is almost negligible around 0.25 Gyr, and from the histograms in age, we can see that there are more low- $\sigma$  CG members with age between  $\sim 2.5$  and 6 Gyr ( $\sim 20\%$  of the galaxies). For the mean value of  $[\alpha/\text{Fe}]$ , the high- $\sigma$  members are  $\sim 0.12$  dex more enhanced than the low- $\sigma$  ones. This is in agreement with the low- $\sigma$  CGs were formed recently compare with the high- $\sigma$  CGs. A more detailed dynamical study for a better understanding of the formation of CGs is required.

#### DISCUSSION AND SUMMARY

# 6.1 Stellar Population Parameters

We investigate the stellar population present in ETGs in the high and low-density environments given by the CGs and field, respectively. Significant differences in the age, metallicity and  $\alpha$ -enrichment of those populations between these two regimes are expected, since the CGs environment is a very favourable environment for interactions, such as mergers. Previously, de La Rosa et al. (2007) suggested that there is a truncation in star formation of ETGs in CGs based on the behaviour of  $[\alpha/Fe]$  versus central velocity dispersion ( $[\alpha/Fe]$  is smaller for larger velocity dispersion – Figure 8). It is important to keep in mind that these results come from a small sample of 22 ETGs

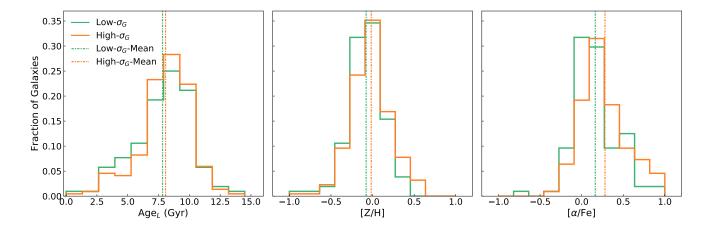


Figure 16. The stellar population parameters of the ETGs in the high and low- $\sigma$  groups. The dashed line is the mean values of the parameter. The p-value calculated for the distribution of the parameters [Z/H] (p = 0.027) and [ $\alpha$ /Fe](p = 0.001) in the Permutation Test suggests the rejection of the null hypothesis which claims that the parameters distributions are from the same parent population. For the age parameter, the p-value = 0.341 it is an indication that the distributions are similar.

in Hickson Compact Groups. However, as presented in Section 3.4 and in Figure 5, our results do not support such interpretation, since  $\lceil \alpha/Fe \rceil$  was shown to increase for higher central velocity dispersion.

Motivated by the morphology-density relation (Dressler 1980) and the Butcher-Oemler effect (Butcher & Oemler 1978), we compare the properties of ETGs in CGs with those in other environments probing a large domain in spatial density. La Barbera et al. (2014) studied a sample of 20,977 bonafide central and satellites ETGs as given in the catalog of Yang et al. (2007). From the definition adopted, the central are those with the highest stellar mass in the group. The central sample was divided based on the host halo mass (lower and higher than  $\log(M_h/M_\odot)=12.5$  ) while the satellite sample was divided into three parts: 1) those inhabiting a low mass halo ( $log(M_h/M_{\odot} < 14)$ ; 2) those in massive haloes (log  $M_h/M_{\odot} \geqslant 14$ ); and 3) satellites in the outskirts of groups (R > $0.5 R_{200}$ ). The analysis of the stellar population parameters for both samples indicates that only the central galaxies have a dependency with the environment, where central located in high mass halos display younger ages than central in lower mass halos. The satellites show no correlation with the environment except for galaxies in the low-velocity dispersion regime.

In Figure 17 (a), we contrast the stellar population properties of ETGs in CGs with those of field, satellites and centrals in low and high halo mass systems. For a consistent comparison with the results from La Barbera et al. (2014), we estimate the luminosity-weighted metallicity using the spectral fitting approach (Equation 1). The age and  $[\alpha/Fe]$  parameters are estimated for all the environments following the hybrid method mentioned in Sec. 3.4. In general, all the stellar population parameters increase with the velocity dispersion, confirming previous findings that velocity dispersion is the main driver of the stellar populations properties. We also see this trend as a manifestation of the downsizing scenario where massive galaxies formed their stellar content in remote epochs and currently star formation is happening in the low mass systems. This is particularly true for  $\sigma \leqslant 150$  km/s, where it is clear that field ETGs are considerably younger than centrals and ETGs in CGs ( $\Delta$  Age  $\sim 2.3$  Gyr). This behaviour is in agreement with Thomas et al. (2010) who show that the low mass ETGs are more affected by the low-density environments. Age gets lower for centrals and satellites as well, but not as much as for Field ETGs. Regarding the [Z/H] parameter, there is a clear environmental effect with centrals in more massive halos being more metal-rich than field ETGs with the difference reaching  $\Delta[Z/H]\sim0.16$  dex. ETGs in CGs seem to fall in between these two classes. Finally, the behavior of [ $\alpha$ /Fe] parameter shows some interesting features. It is slightly higher for centrals when compared to Field and CG galaxies ( $\sim0.1$  dex) up to  $\sigma\sim210$  km/s . However, for  $\sigma\gtrsim250$  km/s [ $\alpha$ /Fe] for ETGs in CGs increases by almost 0.4 dex. This very clear trend may be interpreted as a sign of truncation of the star formation and this may be due to dry merge happening at an early phase of CG formation. It is important to stress that this is the first time that a clear difference between properties of ETGs in CGs and other environments is found.

As far as the comparison to the satellite systems is concerned we are restricted to  $\sigma$  between 100 - 250 km/s since for the extremes there is no corresponding data points in the satellite sample. In this central velocity dispersion range, the age behaves similarly as in the comparison with centrals, with ETGs in the Field being younger for  $\sigma$  < 150 km/s ( $\Delta$ Age ~ 4 Gyr) . Satellite galaxies in the outskirts of groups (for  $R/R_{200} > 0.5$ ) assume ages closest to the field sample as is expected since this sample represents an environment closer and closer to the Field galaxies (low density regime). As for the [Z/H] parameter, we find an increasing tendency for all environments, namely [Z/H] increases monotonically towards more massive galaxies. Notice, however, that Field ETGs tend to be more metal poor than ETGs in other environments. In the case  $[\alpha/\text{Fe}]$ , we see a well established linear relation for satellites in all different groups, as previously found by La Barbera et al. (2014). For the velocity dispersion range of 100 to 250 km/s there is an offset of  $\Delta[Z/H] \sim 0.1$  dex, which may be indicating the well-known quenching process acting in satellite galaxies whose consequence is the suppression of the star formation. This quenching mechanism may be caused ram pressure or frequent high-speed interactions with members of the group.

Finally, it is important to emphasize that our samples of ETGs in CGs and in the Field, exhibit the same trend for the three stellar population parameters, with the exception for the age at the low- $\sigma$  regime and  $[\alpha/\text{Fe}]$  at the high mass end. The low-mass ETGs are younger in the low-density environment (Field) while more massive

ETGs in CGs seem to suffer star formation truncation that leads to an increase in  $[\alpha/Fe]$  when compared to Field galaxies.

#### 6.2 Gas ionization

Given the nature of CGs (moderate velocity dispersion and high number densities) it is expected that galaxy interactions occur frequently and those interactions could trigger the activity in galactic nuclei by channeling the gas to the central region of the galaxies and enhancing star formation. But it is still an open debate the influence of the interactions as a feeding process of SMBHs, and many works have indicated that the fraction of AGN in high density environments could even be smaller than in the less dense environments (ex:Dressler, Smail & Poggianti (1999) and Martini et al. (2007)). Studying galaxies in HCGs, Coziol et al. (1998), Gallagher et al. (2008) and Martínez et al. (2010) estimated a higher fraction of AGN (between 41% and 54%) in those groups compared to other environments. However, Sabater et al. (2012), found no difference between the AGN fraction estimated for their sample of isolated galaxies and that estimated by Martínez et al. (2010) for galaxies in CGs.

Based on the WHAN diagram, we find that the emission lines present in ETGs of our sample are due to the presence of HOLMES. This may indicate that dry merge in CGs is the main mechanism if merger is as effective as it is expected. Also, we see a clear trend in the sense that higher velocity dispersion ETGs are closer to the passive region in the WHAN diagram, implying a softening of the ionization field or a lower overall gas abundance. However, we do not see any significant contribution of ongoing star formation or ionization from AGN in CGs. On the other hand, an overall increase in  $H\alpha$  emission is detected for the field sample, in particular at very low velocity dispersions. This implies that differences between low and high density regimes are not significant as far as the ionization field is concerned, but suggest a higher gas abundance in field galaxies in comparison to galaxies in CGs. One possible explanation for this feature is the occurrence of modest gas loss in CGs due to tidal interactions, which could preserve intact the stellar population properties. This would explain why we do not detect pronounced differences in mean stellar age, metallicity and alpha enrichment between galaxies in CGs and in the field.

# 6.3 Dynamics

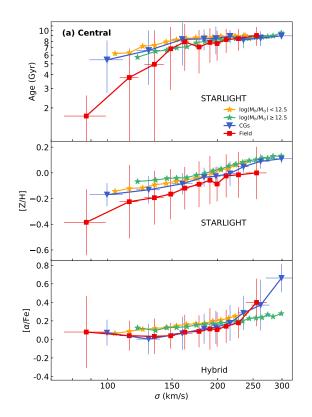
The CGs have their dynamics associated with galaxy-galaxy interactions, mainly merger process and tidal interactions. It is expected by the fast merger model (Mendes de Oliveira and Hickson 1994; Gómez-Flechoso & Domínguez-Tenreiro 2001) that CGs become a giant elliptical galaxy as result of multiple merging events. In this sense, it is reasonable to assume that CGs contribute to the ETG field population. However, it is still a matter of dispute what is the timescale for the evolution of a typical CG. Our dynamical analysis indicate that our sample of 151 CGs may be separated into two groups according to their velocity dispersions (high and low  $\sigma_G$ groups). We distinguish these two dynamical stages as follows: 1) the high- $\sigma$  groups as bound systems in virial equilibrium; and 2) the low-  $\sigma$  groups as associations that probably formed more recently. The low- $\sigma$  groups could be taken as chance alignments (Mamon 2000), but this not seem to be the case. The relation of the absolute magnitude of the groups versus the velocity dispersion shown in Figure 18 is linear for the whole  $\sigma_G$  regime as expected for bound systems.

The high- $\sigma$  groups are more luminous and have more ETGs (~ 76%) than the low- $\sigma$  groups (~ 67%). We also find, as already stated in the works of Hickson, Kindl & Huchra (1988), Ribeiro et al. (1998) and Coziol, Brinks & Bravo-Alfaro (2004), that the fraction of spirals decreases for groups with higher velocity dispersion and that groups in the high- $\sigma$  regime have also smaller crossing times. Since these groups also have a low spiral fraction, it is reasonable to conclude that high- $\sigma$  groups are dynamically old structures. Another important piece of information reinforcing the presence of two families of CGs is the fact that the ETGs in these two families have exhibited stellar population properties significantly different.

# 6.4 Summary

We have performed a study of the galaxy stellar population parameters, the gas ionization and the dynamical properties of 151 CGs from the catalog defined by McConnachie et el. (2009). Our results can be summarized as follows:

- (i) The stellar populations in ETGs belonging to CGs present the same behavior as ETGs in the field following the analysis of the parameters Age, [Z/H] and [ $\alpha$ /Fe], indicating that spatial density is not responsible for establishing the stellar content of these systems. We do not confirm the truncation in star formation observed by de La Rosa et al. (2007). It is worthy to note that the results shown by de La Rosa et al. (2007) are based in a rather small sample composed of 22 ETGs in CGs. In our results, we find that [ $\alpha$ /Fe] increases with central velocity dispersion of the ETGs in both environments, CGs and field.
- (ii) Comparing ETGs in CGs with similar systems in low and high mass halos, we find essentially the same trend of Age, [Z/H] and  $[\alpha/Fe]$  with central velocity dispersion. Considering that we are probing four orders of magnitude in environmental density (from field to centrals), the similarity of these trends may imply a high regularity in the physical process that establishes the stellar population.
- (iii) Examining the behavior of Age as a function of central velocity dispersion we notice that in the low- $\sigma$  regime the less dense is the environment the younger is the stellar population in it. This suggests that quenching may depend on the environment systems with higher halo mass stop star formation more efficiently. On the other hand, looking at the high- $\sigma$  end (> 250 km/s) we find that ETGs in CGs have [ $\alpha$ /Fe] ~0.2 dex greater than centrals inhabiting high mass halos, indicating truncation in star formation for the ETGs in CGs.
- (iv) We identify in our sample of 151 CGs two main families: the low- $\sigma_G$  groups ( $\sigma_G \leqslant 181$  km/s) with larger crossing times and higher fractions of spirals which can be interpreted as recently formed groups while the high- $\sigma$  groups, with smaller crossing times and smaller spiral fraction are those supposedly in virial equilibrium;
- (v) Analysis of the stacked spectra of ETGs in CGs and in the field have shown that these galaxies are located in the same part of the WHAN diagnostic diagram. We see that the ionization source is similar for ETGs in CGs and in the field, with no detectable contribution of ongoing star formation or ionization by a SMBH for galaxies in CGs. Therefore, there are no differences between dense and low-density environments regarding the gas ionizating agent, but the overall gas emission is more intense in field galaxies than in their CG counterparts, hinting at a gas-loss mechanism operating in the CG environment, like tidal interactions.



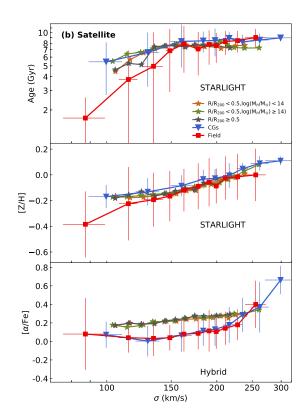


Figure 17. Comparison between the stellar population parameters for central (a) and satellites ETGs (b) defined in La Barbera et al. (2014) and our sample of ETGs in GCs and the field. In La Barbera et al. (2014) the environment is defined by the dark matter halo mass and the central are those galaxies with higher stellar masses from the Yang et al. (2007) catalog. In panel (a) the central embedded in low halo mass ( $\log M_h/M_\odot < 12.5$ ) are consider the "isolated" central while the central in massive halo ( $\log(M_h/M_\odot) \ge 12.5$ ) are the "group" central. For panel (b), the satellite sample are divided in three sub-samples: satellites embedded in low mass halo ( $R/R_{200} < 0.5 \log M_h/M_\odot < 14$ ), massive haloes ( $R/R_{200} < 0.5 \log M_h/M_\odot > 14$ ) and satellites in more external regions of the group ( $R/R_{200} \ge 0.5$ ). To compare with the results from La Barbera et al. (2014), we use the age and [Z/H] from the spectral fitting and the [ $\alpha$ /Fe] from the hybrid method.

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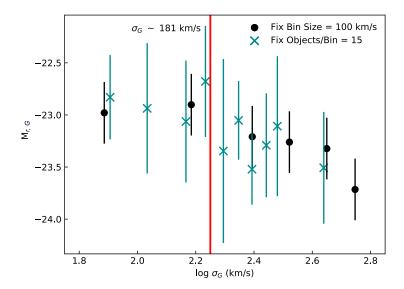


Figure 18. The relation between the absolute magnitude of the group and the velocity dispersion. We use a fix size of bin ( $\Delta = 100$  km/s) and fix number of objects per bin (N/bin = 15) and in both cases the relation is linear.

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**Table A1.** A brief resume of the possible classes attributed in Galaxy Zoo 2. More details at Willett et al. (2013).

Class	Description
Ec	Elliptical completely round
Ec	Elliptical with cigar shape
Ei	Elliptical with shape between round and cigar
Ser	Edge-on spiral with round bulge
Seb	Edge-on spiral with boxy shape bulge
Sen	Edge-on spiral with no bulge
Sa	Spiral with dominant bulge
Sb	Spiral with obvious bulge
Sc	Spiral with noticeable bulge
Sd	Spiral with no bulge
SBa	Barred spiral with dominant bulge
SBb	Barred spiral with obvious bulge
SBc	Barred spiral with just noticeable bulge
SBd	Barred spiral with no bulge

# APPENDIX A: TABLES

# **A1** Morphological Classification Tables

# **A2** Dynamics Properties

Table A2: Dynamical parameters for the CGs of the sample. In each column we have: (1) the identification of each group; (2) number of members in each group; (3) total absolute magnitude of the group in the r-band; (4) velocity dispersion of the group; (5) harmonic radius (Mpc); (6) total dynamical mass (in  $M_{\odot}$ ); (7) the crossing time (in  $H_0^{-1}$ ); (8) spatial density; (9) spiral fraction and (10) dynamical class, either low- $\sigma$  (L) or high- $\sigma$  (H).

GroupID	Nm	$\mathrm{M}_{r,G}$	$\sigma$	$R_{harm}$	log M	$t_{C}$	$\log \rho$	$f_{sp}$	Class
1327	4	-21.32059	164.30531	0.03422	11.80918	0.01531	4.3773	0.5	L
70	4	-23.32746	155.6021	0.0516	11.94032	0.02438	3.84206	0.25	L
510	4	-22.23048	153.97421	0.0631	12.01857	0.03012	3.57991	0.25	L
326	4	-23.43101	161.23244	0.06725	12.08627	0.03066	3.49682	0.0	L
820	4	-22.66269	92.04479	0.03939	11.367	0.03146	4.19393	0.75	L
2209	4	-22.17205	158.51787	0.07893	12.14104	0.0366	3.28828	0.75	L
321	4	-23.09429	153.17699	0.08118	12.12346	0.03896	3.2517	0.0	L
389	4	-22.52972	159.66516	0.09252	12.21629	0.04259	3.08133	0.0	L
113	4	-22.46142	129.23766	0.09071	12.02408	0.05159	3.10703	0.5	L
633	4	-23.07535	130.62134	0.10499	12.09681	0.05908	2.91659	0.25	L
1114	6	-22.67863	158.65254	0.13108	12.36209	0.06074	2.80343	0.33	L
1616	4	-22.49507	170.37962	0.14116	12.45621	0.0609	2.53081	0.25	L
252	4	-23.55476	134.75757	0.12162	12.18777	0.06634	2.72494	0.25	L
904	4	-23.23118	144.67075	0.13194	12.28478	0.06704	2.61886	0.25	L
1409	4	-23.17326	121.24132	0.11638	12.07683	0.07056	2.78233	0.25	L
1063	4	-22.63152	104.22949	0.10803	11.91319	0.07619	2.87931	0.75	L
1458	4	-22.29223	146.67732	0.15218	12.35874	0.07627	2.43288	0.25	L
1385	4	-22.77454	144.35689	0.15482	12.35237	0.07884	2.41046	0.0	L
1059	4	-22.41693	134.353	0.1444	12.25973	0.07901	2.50123	0.0	L
724	4	-23.37203	176.75452	0.19093	12.61926	0.07941	2.13736	0.0	L
1185	4	-23.22581	153.71902	0.16608	12.43742	0.07942	2.31903	0.5	L
425	4	-22.74902	165.96463	0.1797	12.53824	0.0796	2.21629	0.25	L
1011	4	-23.62991	156.5828	0.17335	12.47206	0.08138	2.26323	0.25	L
728	4	-21.8888	78.10072	0.08706	11.56879	0.08194	3.16049	0.0	L
2139	5	-22.6674	171.11082	0.19777	12.60637	0.08496	2.1884	0.4	L
1090	4	-22.38491	119.03671	0.14001	12.14117	0.08646	2.54151	0.25	L
1434	4	-22.13416	128.16104	0.15158	12.23982	0.08695	2.438	0.25	L
1895	5	-23.5568	108.89929	0.14542	12.08033	0.09816	2.58899	0.4	L
1767	5	-23.67012	94.37662	0.13608	11.92716	0.10599	2.67553	0.2	L
952	4	-23.06343	151.19118	0.22288	12.55078	0.10837	1.93575	0.5	L
1004	4	-23.16966	172.05598	0.27225	12.74996	0.11632	1.67508	0.25	L
1539	4	-22.97823	117.10299	0.19011	12.2598	0.11934	2.14293	0.5	L
1783	4	-22.59076	57.29758	0.0973	11.34805	0.12484	3.0156	0.5	L
1020	4	-22.65908	97.0623	0.17318	12.05625	0.13116	2.26447	0.0	L
2021	4	-22.96518	156.2697	0.28007	12.67867	0.13175	1.63816	0.75	L
2011	4	-23.70521	94.6297	0.17977	12.05043	0.13965	2.21582	0.5	L
1886	4	-22.30497	119.47761	0.22944	12.35889	0.14116	1.89798	1.0	L
1163	4	-23.14993	82.52488	0.16134	11.88458	0.14372	2.35671	0.75	L
1371	5	-23.5258	124.59372	0.24885	12.43058	0.14682	1.88909	0.0	L
2155	4	-21.92206	120.5286	0.24101	12.38787	0.14699	1.83386	0.0	L
1202	4	-23.53411	80.5443	0.16772	11.8803	0.15307	2.30625	0.25	L
1553	4	-22.93678	92.58204	0.19447	12.06557	0.15441	2.11338	0.5	L
1153	4	-23.24351	102.1831	0.22063	12.20607	0.15872	1.949	0.5	L
1858	4	-23.18516	59.49733	0.13608	11.52643	0.16813	2.57863	0.5	L
1109	4	-22.67949	88.81782	0.21703	12.07718	0.17963	1.97039	1.0	L
1667	4	-22.44853	97.20513	0.23881	12.19709	0.1806	1.84579	0.75	L
1605	4	-22.83016	80.76373	0.20159	11.96256	0.18349	2.06655	0.25	L
1075	4 4	-22.80477	91.26037	0.24006	12.14454	0.19337	1.83901	0.0	L
2149		-22.63643	81.35825	0.22432	12.01533	0.20269	1.92734	0.0	L
2078	4	-22.92845	107.98608	0.32292	12.41948	0.21982	1.4527	0.25	L
2176	4	-23.13365	92.03265	0.2929	12.23825	0.23395	1.57982	0.0	L
1264	4	-22.7586	39.24533	0.12627	11.13254	0.23652	2.67604	0.0	L
1213	5	-23.26164	59.47038	0.19653	11.68568	0.24293	2.1966	0.2	L
1987	5	-23.24915	66.6158	0.23337	11.85885	0.25752	1.97277	0.6	L
2202	4	-23.80747	54.25206	0.42696	11.94288	0.57853	1.08879	0.0	L
1217	4 5	-23.39339 -23.52758	579.8492 579.21275	0.08246	13.28653	0.01045	3.23124	0.25	Н
559 42	5 4		578.21375	0.0878 $0.07248$	13.31133	0.01116	3.24637	0.4	Н
42 481	4	-23.35465	429.73114		12.97029	0.0124	3.39925	0.0	Н
481 90	4	-22.98172 -23.77042	264.16525 417.0572	0.04732 0.08009	12.36249 12.9876	0.01317 0.01412	3.9547 3.26931	0.5 0.0	H H
90 1265	4	-23.77042 -21.96506	205.35538	0.08009	12.9876	0.01412	3.26931 4.14632	0.0	н Н
1265 1494	4	-21.96506	203.33338 559.589	0.04083		0.01462	4.14632 2.84035	0.23	н Н
1474	4	-23.10810	227.269	0.11131	13.38593	0.01402	2.04033	0.5	п

	Table A2 – continued from previous page									
Section   Sect			$M_{r,G}$		$R_{harm}$		$t_C$			Class
1926					0.06344					
140										
1376										
13366   4										
1774										
The color of the										
1565	1036	4	-22.01109		0.08887			3.13365		
1249										
2027   5										
594   5   -22.39405   279.22214   0.10583   12.76016   0.02786   3.00304   0.0   H   1407   4   -23.86561   498.62305   0.1914   13.52126   0.02823   2.13378   0.0   H   1508   4   -22.76212   302.03862   0.11641   12.86983   0.02833   2.78199   0.0   H   1508   4   -22.151397   247.17389   0.09902   12.62538   0.02945   2.99281   0.75   H   1605   4   -22.4337   407.35153   0.16523   13.28167   0.02982   2.32573   1.0   H   19065   4   -22.43373   40.31396   0.14233   13.28167   0.02982   2.32573   1.0   H   1908   1.0		4								
1407		5								
508         4         -22,76212         302,03862         0.11641         12,86983         0,02833         2,78199         0.0         H           1372         4         -22,151397         247,17389         0,09902         12,62538         0,02945         2,99281         0.75         H           1065         4         -22,43837         407,35153         0,16523         13,28167         0,02982         2,2573         1,0         H           2083         4         -22,30191         191,67117         0,07827         12,30235         0,03002         3,29922         0,75         H           1390         5         -23,84172         298,29538         0,1333         12,93825         0,03831         2,86299         0.0         H           1169         5         -23,36415         301,94986         0,13968         12,94867         0,03401         2,54453         0,25         0         H           42,32,3611         301,94986         0,13968         12,94867         0,03425         2,6428         0         0         H           1713         4         -23,8475         442,3833         0,2142         13,46039         0,03513         2,04455         0         0         H										
1372										
2056										
933         4         -22,30191         191,67117         0.07827         12,30235         0.03002         3.29922         0.75         H           2083         4         -22,49336         340,31396         0.14233         13,06071         0.03074         2.52009         0.25         H           773         5         -22,77582         303,24048         0.1353         12,93852         0.0328         2.68299         0.0         H           1169         5         -23,70444         192,53825         0.08835         12,35889         0.03373         3.28826         0.0         H           657         4         -23,36415         301,94986         0.13968         12,94867         0.03401         2.54463         0.25         H           850         4         -23,4875         442,3833         0.21142         13,46039         0.03513         2.0455         0.0         H           1705         4         -22,3627         275,7555         0.1341         12,84989         0.03556         2.60441         0.0         H           1214         4         -23,99199         210,16231         1.0154         12,51161         0.03682         2.83045         0.0         H										
2083		4	-22.43837	407.35153	0.16523	13.28167		2.32573	1.0	Н
1773   5   -22,77582   303,24048   0,1353   12,93852   0,0328   2,68829   0,0   H   1789   5   -23,84172   298,29538   0,13478   12,92256   0,03373   2,32826   0,0   H   169   5   -23,70944   192,53825   0,08835   12,35889   0,03373   3,23826   0,0   H   1667   4   -23,36415   301,54986   0,13968   12,94867   0,03401   2,54453   0,25   H   179   1880   4   -23,4875   442,3833   0,21142   13,46039   0,03513   2,00455   0,0   H   1705   4   -22,3627   275,7555   0,13341   12,84989   0,03552   2,54403   0,5   H   1705   4   -22,3627   275,7555   0,13341   12,84989   0,03552   2,54403   0,5   H   1705   4   -22,3627   275,7555   0,13341   12,84989   0,03556   2,60441   0,0   H   1214   4   -23,99199   210,16231   0,1054   12,51161   0,03687   2,91143   0,25   H   124   4   -23,99199   210,16231   0,1054   12,51161   0,03687   2,91143   0,25   H   125   4   -22,26273   242,17967   0,12405   12,75535   0,03745   2,55056   0,25   H   125   4   -23,32515   255,17973   0,13352   12,78288   0,03846   2,60335   0,0   H   13686   4   -23,84638   245,40575   0,13142   12,74207   0,03937   2,62402   0,25   H   1686   4   -23,84638   245,40575   0,13142   12,74207   0,03937   2,62402   0,25   H   1686   4   -23,45498   251,71504   0,1405   12,79313   0,04103   2,53698   0,0   H   1803   4   -22,29249   20,34158   0,12253   12,61899   0,04088   2,71522   0,25   H   1406   4   -23,74362   240,54518   0,13825   12,74671   0,04225   2,55799   0,25   H   1666   5   -24,16096   469,9154   0,2986   13,66287   0,04672   1,56135   0,0   H   1324   4   -23,08334   230,19572   0,14081   12,71649   0,04497   2,53403   0,75   H   1324   4   -23,33909   260,70352   0,1608   12,87422   0,04571   2,36207   0,0   H   1324   4   -23,38991   24,60916   469,9154   0,29866   13,66287   0,04672   1,56135   0,4   H   1324   4   -23,38991   24,40796   0,14081   12,71649   0,04497   2,53450   0,0   H   1324   4   -23,38991   24,60916   4,0916   4,0916   4,0916   4,0916   4,0916   4,0916   4,0916   4,0916   4,0916   4,0916   4,0916   4,0916   4,0916										
1390   5   -23,84172   298,29538   0.13478   12,92256   0.03321   2,68804   0.2   H										
169   5   -23,70944   192,53825   0,08835   12,35889   0,03373   3,23826   0,0   H		5								
657         4         -23.36415         301.94986         0.13968         12.94867         0.03401         2.54453         0.25         H           850         4         -23.4875         442.3833         0.21142         13.46039         0.03513         2.00455         0.0         H           1713         4         -22.87173         291.43262         0.13974         12.91804         0.03525         2.54403         0.5         H           1713         4         -22.9522         226.38466         0.11216         12.91804         0.03525         2.54403         0.5         H           618         4         -22.9522         226.38466         0.11216         12.60319         0.03642         2.83045         0.0         H           1214         -23.20133         273.20392         0.13904         12.85976         0.03741         2.55056         0.25         H           209         4         -22.26273         242.17967         0.12405         12.70553         0.03765         2.69917         0.25         H           375         4         -22.17997         208.71983         0.11107         12.52836         0.03912         2.84323         0.5         H           1686 <td></td> <td>5</td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td> <td></td>		5								
3800         4         -23,29121         284,13666         0.1324         12,8726         0.03425         2.61428         0.755         H           1713         4         -22,8173         291,43262         0.13974         12,91804         0.03525         2.54403         0.5         H           1705         4         -22,3627         275,7555         0.13341         12,84989         0.03556         2.60441         0.0         H           618         4         -22,9252         226,83466         0.11216         12,60319         0.03687         2.81045         0.0         H           1214         4         -23,99199         210,16231         0.1054         12,51161         0.03687         2.91143         0.25         H           209         4         -22,26273         242,17967         0.12405         12,70553         0.03765         269917         0.25         H           225         4         -23,32515         255,17973         0.13352         12,78288         0.03846         2.60335         0.0         H           1686         4         -23,84638         245,40575         0.13142         12,74207         0.03937         2.62402         0.25         H										
850         4         -23.4875         442.3833         0.21142         13.46039         0.03513         2.00455         0.0         H           1713         4         -22.87173         291.43262         0.13974         12.91804         0.03525         2.54403         0.5         H           1705         4         -22.9252         226.38466         0.11216         12.60319         0.03642         2.83045         0.0         H           1214         4         -23.99199         210.16231         0.1054         12.51161         0.03687         2.91143         0.25         H           209         4         -22.26273         242.17967         0.12405         12.70553         0.03761         2.59076         0.25         H           209         4         -22.26273         242.17967         0.12405         12.70553         0.03765         2.69917         0.25         H           209         4         -22.26673         242.17987         0.12405         12.70553         0.03761         2.59017         0.25         H           375         4         -22.17997         208.71983         0.11107         12.52836         0.03912         2.84323         0.5         H										
1713										
1705										
1214										
596         4         -23,20133         273,20392         0.13904         12,85976         0.03741         2,55056         0.25         H           209         4         -22,26273         242,17967         0.12405         12,70553         0.03765         2,69917         0.25         H           225         4         -23,32515         255,17973         0.13162         12,78288         0.03846         2,60335         0.0         H           1686         4         -23,84638         245,40575         0.13142         12,74207         0.03937         2,62402         0.25         H           1686         4         -23,1078         303,56326         0.16704         13,03097         0.04045         2,3115         0.0         H           1303         4         -22,17948         251,71504         0.1405         12,79313         0.04103         2,53698         0.0         H           2256         4         -24,45498         251,71504         0.1405         12,79313         0.04103         2,53698         0.0         H           2087         4         -23,74362         240,54518         0.13825         12,74671         0.04225         2,55799         0.25         H <tr< td=""><td>618</td><td></td><td>-22.9252</td><td>226.38466</td><td>0.11216</td><td>12.60319</td><td>0.03642</td><td>2.83045</td><td>0.0</td><td>Н</td></tr<>	618		-22.9252	226.38466	0.11216	12.60319	0.03642	2.83045	0.0	Н
209         4         -22,26273         242,17967         0,12405         12,70553         0,03765         2,69917         0,25         H           225         4         -23,32515         255,17973         0,13352         12,78288         0,03846         2,60335         0.0         H           375         4         -22,17997         208,71983         0,11107         12,52836         0,03912         2,84323         0.5         H           663         4         -23,84638         245,40575         0,13142         12,74207         0,03937         2,62402         0,25         H           1303         4         -22,29249         220,34158         0,12253         12,61809         0,04088         2,71522         0,25         H           2556         4         -24,45498         251,71504         0,1405         12,79313         0,04103         2,5668         0,0         H           800         4         -22,71132         232,23518         0,12979         12,68875         0,04108         2,64025         0,25         H           2087         4         -23,05776         185,30817         0,11045         12,42261         0,04382         2,85040         0,0         H <tr< td=""><td></td><td></td><td></td><td></td><td></td><td></td><td>0.03687</td><td>2.91143</td><td></td><td></td></tr<>							0.03687	2.91143		
225         4         -23,32515         255,17973         0.13352         12,78288         0.03846         26,0335         0.0         H           375         4         -22,17997         208,71983         0.11107         12,52836         0.03912         2,84323         0.5         H           1686         4         -23,1078         303,56326         0.16704         13,03097         0.04045         2,3115         0.0         H           1303         4         -22,29249         220,34158         0.12253         12,61809         0.04088         2,71522         0.25         H           800         4         -24,45498         251,71504         0.1405         12,79313         0.04103         2,53698         0.0         H           800         4         -22,71132         232,23518         0.12979         12,68875         0.04108         2,64025         0.25         H           406         4         -23,074362         240,54518         0.13825         12,74671         0.04225         2,55799         0.25         H           2087         4         -23,0833         230,19572         0.14081         12,74671         0.04425         2,53403         0.75         H										
375										
1686         4         -23.84638         245.40575         0.13142         12.74207         0.03937         2.62402         0.25         H           663         4         -23.1078         303.56326         0.16704         13.03097         0.04045         2.3115         0.0         H           1303         4         -22.29249         220.34158         0.12253         12.61809         0.04045         2.3115         0.0         H           800         4         -22.71132         232.23518         0.12979         12.68875         0.04108         2.64025         0.25         H           406         4         -23.05776         185.30817         0.11045         12.42261         0.04225         2.55799         0.25         H           2087         4         -23.05776         185.30817         0.11045         12.24261         0.04382         2.85046         0.0         H           253         4         -23.057003         258.4045         0.16068         12.87422         0.04477         2.53403         0.75         H           2166         5         -24.16096         469.9154         0.29866         13.66287         0.04672         1.65135         0.4         H										
663										
1303										
2256         4         -24.45498         251.71504         0.1405         12.79313         0.04103         2.53698         0.0         H           800         4         -22.71132         232.23518         0.12979         12.68875         0.04108         2.64025         0.25         H           406         4         -23.05776         185.30817         0.11045         12.42261         0.04382         2.85046         0.0         H           253         4         -23.08334         230.19572         0.14081         12.71649         0.04497         2.53403         0.75         H           673         4         -23.07703         258.4045         0.16068         12.87422         0.04571         2.36207         0.0         H           135         4         -23.01472         199.39705         0.12633         12.54459         0.04672         2.67546         0.25         H           2166         5         -24.16096         469.9154         0.29866         13.66287         0.04672         1.65135         0.4         H           1717         4         -23.33999         260.70352         0.16742         12.89976         0.04721         2.30852         0.25         H										
800         4         -22.71132         232.23518         0.12979         12.68875         0.04108         2.64025         0.25         H           406         4         -23.74362         240.54518         0.13825         12.74671         0.04225         2.55799         0.25         H           2087         4         -23.08736         185.30817         0.11045         12.42261         0.04382         2.85046         0.0         H           253         4         -23.08334         230.19572         0.14081         12.71649         0.04497         2.53403         0.75         H           673         4         -23.57003         258.4045         0.16068         12.87422         0.04571         2.36207         0.0         H           1355         4         -23.01472         199.39705         0.12633         12.54459         0.04657         2.67546         0.25         H           2166         5         -24.16096         469.9154         0.29866         13.66287         0.04672         1.65135         0.4         H           1717         4         -23.24431         383.56552         0.24466         13.39989         0.04689         1.8143         0.25         H <t< td=""><td></td><td>4</td><td></td><td></td><td></td><td></td><td></td><td></td><td></td><td></td></t<>		4								
2087         4         -23.05776         185.30817         0.11045         12.42261         0.04382         2.85046         0.0         H           253         4         -23.08334         230.19572         0.14081         12.71649         0.04497         2.53403         0.75         H           673         4         -23.57003         258.4045         0.16068         12.87422         0.04571         2.36207         0.0         H           135         4         -23.01472         199.39705         0.12633         12.54459         0.04657         2.67546         0.25         H           2166         5         -24.16096         469.9154         0.29866         13.66287         0.04672         1.65135         0.4         H           1717         4         -23.33909         260.70352         0.16742         12.89976         0.04689         1.8143         0.25         H           670         5         -24.18419         377.83524         0.24745         13.39175         0.04814         1.89641         0.2         H           748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H	800	4		232.23518			0.04108	2.64025		Н
253         4         -23.08334         230.19572         0.14081         12.71649         0.04497         2.53403         0.75         H           673         4         -23.57003         258.4045         0.16068         12.87422         0.04571         2.36207         0.0         H           135         4         -23.01472         199.39705         0.12633         12.54459         0.04657         2.67546         0.25         H           2166         5         -24.16096         469.9154         0.29866         13.66287         0.04672         1.65135         0.4         H           1717         4         -23.24431         383.56552         0.24466         13.39989         0.04689         1.8143         0.25         H           1324         4         -23.33909         260.70352         0.16742         12.89976         0.04721         2.30852         0.25         H           748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H           895         4         -22.32889         194.40796         0.14087         12.5699         0.05327         2.53351         0.0         H										
673         4         -23.57003         258.4045         0.16068         12.87422         0.04571         2.36207         0.0         H           135         4         -23.01472         199.39705         0.12633         12.54459         0.04657         2.67546         0.25         H           2166         5         -24.16096         469.9154         0.29866         13.66287         0.04672         1.65135         0.4         H           1717         4         -23.24431         383.56552         0.24466         13.39989         0.04689         1.8143         0.25         H           670         5         -24.18419         377.83524         0.24745         13.39175         0.04814         1.89641         0.2         H           748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H           895         4         -22.32889         194.40796         0.14087         12.5699         0.05327         2.53351         0.0         H           1070         4         -22.38892         248.3479         0.18542         12.90193         0.05488         2.17549         0.0         H										
135         4         -23.01472         199.39705         0.12633         12.54459         0.04657         2.67546         0.25         H           2166         5         -24.16096         469.9154         0.29866         13.66287         0.04672         1.65135         0.4         H           1717         4         -23.24431         383.56552         0.24466         13.39989         0.04689         1.8143         0.25         H           1324         4         -23.3909         260.70352         0.16742         12.89976         0.04721         2.30852         0.25         H           670         5         -24.18419         377.83524         0.24745         13.39175         0.04814         1.89641         0.2         H           748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H           895         4         -22.32889         194.40796         0.14087         12.5699         0.05327         2.53351         0.0         H           1070         4         -22.89126         248.3479         0.18542         12.90193         0.05488         2.17549         0.0         1										
2166         5         -24.16096         469.9154         0.29866         13.66287         0.04672         1.65135         0.4         H           1717         4         -23.24431         383.56552         0.24466         13.39989         0.04689         1.8143         0.25         H           1324         4         -23.33909         260.70352         0.16742         12.89976         0.04721         2.30852         0.25         H           670         5         -24.18419         377.83524         0.24745         13.39175         0.04814         1.89641         0.2         H           748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H           895         4         -22.32889         194.40796         0.14087         12.5699         0.05327         2.53351         0.0         H           1070         4         -22.89126         248.3479         0.18542         12.90193         0.05488         2.17549         0.0         H           1274         4         -22.9272         275.12704         0.20876         13.04236         0.05578         2.02105         0.5         H										
1717         4         -23.24431         383.56552         0.24466         13.39989         0.04689         1.8143         0.25         H           1324         4         -23.33909         260.70352         0.16742         12.89976         0.04721         2.30852         0.25         H           670         5         -24.18419         377.83524         0.24745         13.39175         0.04814         1.89641         0.2         H           748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H           895         4         -22.32889         194.40796         0.14087         12.5699         0.05327         2.53351         0.0         H           1070         4         -22.89126         248.3479         0.18542         12.90193         0.05488         2.17549         0.0         H           1274         4         -22.9272         275.12704         0.20876         13.04236         0.05578         2.02105         0.5         H           1113         4         -23.30823         218.56764         0.16728         12.74627         0.05626         2.30962         0.25         H										
1324         4         -23.33909         260.70352         0.16742         12.89976         0.04721         2.30852         0.25         H           670         5         -24.18419         377.83524         0.24745         13.39175         0.04814         1.89641         0.2         H           748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H           895         4         -22.32889         194.40796         0.14087         12.5699         0.05327         2.53351         0.0         H           1070         4         -22.89126         248.3479         0.18542         12.90193         0.05488         2.17549         0.0         H           1274         4         -22.9272         275.12704         0.20876         13.04236         0.05578         2.02105         0.5         H           1113         4         -23.30823         218.56764         0.16728         12.74627         0.05626         2.30962         0.25         H           208         5         -23.81562         276.8277         0.21869         13.0679         0.05807         2.05741         0.2         H		-								
670         5         -24.18419         377.83524         0.24745         13.39175         0.04814         1.89641         0.2         H           748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H           895         4         -22.32889         194.40796         0.14087         12.5699         0.05327         2.53351         0.0         H           1070         4         -22.89126         248.3479         0.18542         12.90193         0.05488         2.17549         0.0         H           1274         4         -22.9272         275.12704         0.20876         13.04236         0.05578         2.02105         0.5         H           1113         4         -23.30823         218.56764         0.16728         12.74627         0.05626         2.30962         0.25         H           2208         5         -23.81562         276.8277         0.21869         13.0679         0.05807         2.05741         0.2         H           1300         4         -22.30241         183.40327         0.15063         12.54837         0.06037         2.44627         0.5         H										
748         5         -23.80492         318.838         0.21586         13.18497         0.04977         2.07436         0.2         H           895         4         -22.32889         194.40796         0.14087         12.5699         0.05327         2.53351         0.0         H           1070         4         -22.89126         248.3479         0.18542         12.90193         0.05488         2.17549         0.0         H           1274         4         -22.9272         275.12704         0.20876         13.04236         0.05578         2.02105         0.5         H           1113         4         -23.30823         218.56764         0.16728         12.74627         0.05626         2.30962         0.25         H           2208         5         -23.81562         276.8277         0.21869         13.0679         0.05807         2.05741         0.2         H           1300         4         -22.30241         183.40327         0.15063         12.54837         0.06037         2.44627         0.5         H           1592         4         -23.52712         286.63342         0.23863         13.13602         0.0612         1.84682         0.25         H		5								
1070         4         -22.89126         248.3479         0.18542         12.90193         0.05488         2.17549         0.0         H           1274         4         -22.9272         275.12704         0.20876         13.04236         0.05578         2.02105         0.5         H           1113         4         -23.30823         218.56764         0.16728         12.74627         0.05626         2.30962         0.25         H           2208         5         -23.81562         276.8277         0.21869         13.0679         0.05807         2.05741         0.2         H           1300         4         -22.30241         183.40327         0.15063         12.54837         0.06037         2.44627         0.5         H           920         4         -23.52712         286.63342         0.23863         13.13602         0.0612         1.84682         0.25         H           1592         4         -22.70905         191.5309         0.16128         12.61572         0.0619         2.35719         0.5         H           1769         4         -23.88926         283.71918         0.24039         13.13035         0.06228         1.83722         0.25         H	748	5	-23.80492	318.838	0.21586	13.18497	0.04977	2.07436	0.2	Н
1274         4         -22.9272         275.12704         0.20876         13.04236         0.05578         2.02105         0.5         H           1113         4         -23.30823         218.56764         0.16728         12.74627         0.05626         2.30962         0.25         H           2208         5         -23.81562         276.8277         0.21869         13.0679         0.05807         2.05741         0.2         H           1300         4         -22.30241         183.40327         0.15063         12.54837         0.06037         2.44627         0.5         H           920         4         -23.52712         286.63342         0.23863         13.13602         0.0612         1.84682         0.25         H           1592         4         -22.70905         191.5309         0.16128         12.61572         0.0619         2.35719         0.5         H           1769         4         -23.88926         283.71918         0.24039         13.13035         0.06228         1.83722         0.25         H           1464         4         -22.71718         215.32292         0.18275         12.77169         0.06239         2.1944         0.5         H										
1113         4         -23.30823         218.56764         0.16728         12.74627         0.05626         2.30962         0.25         H           2208         5         -23.81562         276.8277         0.21869         13.0679         0.05807         2.05741         0.2         H           1300         4         -22.30241         183.40327         0.15063         12.54837         0.06037         2.44627         0.5         H           920         4         -23.52712         286.63342         0.23863         13.13602         0.0612         1.84682         0.25         H           1592         4         -22.70905         191.5309         0.16128         12.61572         0.0619         2.35719         0.5         H           1769         4         -23.88926         283.71918         0.24039         13.13035         0.06228         1.83722         0.25         H           1464         4         -22.71718         215.32292         0.18275         12.77169         0.06239         2.1944         0.5         H           811         4         -22.4584         222.37167         0.18961         12.81566         0.06268         2.14642         0.0         H										
2208         5         -23.81562         276.8277         0.21869         13.0679         0.05807         2.05741         0.2         H           1300         4         -22.30241         183.40327         0.15063         12.54837         0.06037         2.44627         0.5         H           920         4         -23.52712         286.63342         0.23863         13.13602         0.0612         1.84682         0.25         H           1592         4         -22.70905         191.5309         0.16128         12.61572         0.0619         2.35719         0.5         H           1769         4         -23.88926         283.71918         0.24039         13.13035         0.06228         1.83722         0.25         H           1464         4         -22.71718         215.32292         0.18275         12.77169         0.06239         2.1944         0.5         H           811         4         -22.4584         222.37167         0.18961         12.81566         0.06239         2.1944         0.5         H           1173         4         -23.81617         276.80832         0.2416         13.1111         0.06416         1.83069         0.0         H										
1300         4         -22.30241         183.40327         0.15063         12.54837         0.06037         2.44627         0.5         H           920         4         -23.52712         286.63342         0.23863         13.13602         0.0612         1.84682         0.25         H           1592         4         -22.70905         191.5309         0.16128         12.61572         0.0619         2.35719         0.5         H           1769         4         -23.88926         283.71918         0.24039         13.13035         0.06228         1.83722         0.25         H           1464         4         -22.71718         215.32292         0.18275         12.77169         0.06239         2.1944         0.5         H           811         4         -22.4584         222.37167         0.18961         12.81566         0.06239         2.1944         0.5         H           1173         4         -23.81617         276.80832         0.2416         13.1111         0.06416         1.83069         0.0         H           1909         5         -23.94225         298.64487         0.26658         13.21979         0.06562         1.79941         0.0         H										
920         4         -23.52712         286.63342         0.23863         13.13602         0.0612         1.84682         0.25         H           1592         4         -22.70905         191.5309         0.16128         12.61572         0.0619         2.35719         0.5         H           1769         4         -23.88926         283.71918         0.24039         13.13035         0.06228         1.83722         0.25         H           1464         4         -22.71718         215.32292         0.18275         12.77169         0.06239         2.1944         0.5         H           811         4         -22.4584         222.37167         0.18961         12.81566         0.06268         2.14642         0.0         H           1173         4         -23.81617         276.80832         0.2416         13.1111         0.06416         1.83069         0.0         H           1909         5         -23.94225         298.64487         0.26658         13.21979         0.06562         1.79941         0.0         H           1012         4         -22.352054         257.65         0.2492         13.06226         0.0711         1.79033         0.25         H										
1592       4       -22.70905       191.5309       0.16128       12.61572       0.0619       2.35719       0.5       H         1769       4       -23.88926       283.71918       0.24039       13.13035       0.06228       1.83722       0.25       H         1464       4       -22.71718       215.32292       0.18275       12.77169       0.06239       2.1944       0.5       H         811       4       -22.4584       222.37167       0.18961       12.81566       0.06268       2.14642       0.0       H         1173       4       -23.81617       276.80832       0.2416       13.1111       0.06416       1.83069       0.0       H         1909       5       -23.94225       298.64487       0.26658       13.21979       0.06562       1.79941       0.0       H         1012       4       -22.36551       210.87572       0.19765       12.78761       0.0689       2.09226       0.5       H         1301       4       -23.52054       257.65       0.2492       13.06226       0.0711       1.79033       0.25       H         735       4       -23.53957       211.2864       0.20515       12.80547       0.07138										
1769       4       -23.88926       283.71918       0.24039       13.13035       0.06228       1.83722       0.25       H         1464       4       -22.71718       215.32292       0.18275       12.77169       0.06239       2.1944       0.5       H         811       4       -22.4584       222.37167       0.18961       12.81566       0.06268       2.14642       0.0       H         1173       4       -23.81617       276.80832       0.2416       13.1111       0.06416       1.83069       0.0       H         1909       5       -23.94225       298.64487       0.26658       13.21979       0.06562       1.79941       0.0       H         1012       4       -22.36551       210.87572       0.19765       12.78761       0.0689       2.09226       0.5       H         1301       4       -23.52054       257.65       0.2492       13.06226       0.0711       1.79033       0.25       H         735       4       -23.53957       211.2864       0.20515       12.80547       0.07138       2.04374       0.25       H         1189       5       -23.13815       233.37009       0.22703       12.93583       0.07151 <td></td>										
811       4       -22.4584       222.37167       0.18961       12.81566       0.06268       2.14642       0.0       H         1173       4       -23.81617       276.80832       0.2416       13.1111       0.06416       1.83069       0.0       H         1909       5       -23.94225       298.64487       0.26658       13.21979       0.06562       1.79941       0.0       H         1012       4       -22.36551       210.87572       0.19765       12.78761       0.0689       2.09226       0.5       H         1301       4       -23.52054       257.65       0.2492       13.06226       0.0711       1.79033       0.25       H         735       4       -23.53957       211.2864       0.20515       12.80547       0.07138       2.04374       0.25       H         1189       5       -23.13815       233.37009       0.22703       12.93583       0.07151       2.00861       0.8       H         1789       4       -23.51063       287.02997       0.28038       13.20725       0.07181       1.63673       0.25       H         1901       4       -23.27581       246.73026       0.24526       13.01772       0.07307 <td>1769</td> <td>4</td> <td></td> <td></td> <td></td> <td></td> <td>0.06228</td> <td>1.83722</td> <td>0.25</td> <td></td>	1769	4					0.06228	1.83722	0.25	
1173       4       -23.81617       276.80832       0.2416       13.1111       0.06416       1.83069       0.0       H         1909       5       -23.94225       298.64487       0.26658       13.21979       0.06562       1.79941       0.0       H         1012       4       -22.36551       210.87572       0.19765       12.78761       0.0689       2.09226       0.5       H         1301       4       -23.52054       257.65       0.2492       13.06226       0.0711       1.79033       0.25       H         735       4       -23.53957       211.2864       0.20515       12.80547       0.07138       2.04374       0.25       H         1189       5       -23.13815       233.37009       0.22703       12.93583       0.07151       2.00861       0.8       H         1789       4       -23.51063       287.02997       0.28038       13.20725       0.07181       1.63673       0.25       H         1901       4       -23.27581       246.73026       0.24526       13.01772       0.07307       1.8111       0.25       H	1464	4				12.77169	0.06239			
1909       5       -23.94225       298.64487       0.26658       13.21979       0.06562       1.79941       0.0       H         1012       4       -22.36551       210.87572       0.19765       12.78761       0.0689       2.09226       0.5       H         1301       4       -23.52054       257.65       0.2492       13.06226       0.0711       1.79033       0.25       H         735       4       -23.53957       211.2864       0.20515       12.80547       0.07138       2.04374       0.25       H         1189       5       -23.13815       233.37009       0.22703       12.93583       0.07151       2.00861       0.8       H         1789       4       -23.51063       287.02997       0.28038       13.20725       0.07181       1.63673       0.25       H         1901       4       -23.27581       246.73026       0.24526       13.01772       0.07307       1.8111       0.25       H										
1012       4       -22.36551       210.87572       0.19765       12.78761       0.0689       2.09226       0.5       H         1301       4       -23.52054       257.65       0.2492       13.06226       0.0711       1.79033       0.25       H         735       4       -23.53957       211.2864       0.20515       12.80547       0.07138       2.04374       0.25       H         1189       5       -23.13815       233.37009       0.22703       12.93583       0.07151       2.00861       0.8       H         1789       4       -23.51063       287.02997       0.28038       13.20725       0.07181       1.63673       0.25       H         1901       4       -23.27581       246.73026       0.24526       13.01772       0.07307       1.8111       0.25       H										
1301       4       -23.52054       257.65       0.2492       13.06226       0.0711       1.79033       0.25       H         735       4       -23.53957       211.2864       0.20515       12.80547       0.07138       2.04374       0.25       H         1189       5       -23.13815       233.37009       0.22703       12.93583       0.07151       2.00861       0.8       H         1789       4       -23.51063       287.02997       0.28038       13.20725       0.07181       1.63673       0.25       H         1901       4       -23.27581       246.73026       0.24526       13.01772       0.07307       1.8111       0.25       H										
735       4       -23.53957       211.2864       0.20515       12.80547       0.07138       2.04374       0.25       H         1189       5       -23.13815       233.37009       0.22703       12.93583       0.07151       2.00861       0.8       H         1789       4       -23.51063       287.02997       0.28038       13.20725       0.07181       1.63673       0.25       H         1901       4       -23.27581       246.73026       0.24526       13.01772       0.07307       1.8111       0.25       H										
1189       5       -23.13815       233.37009       0.22703       12.93583       0.07151       2.00861       0.8       H         1789       4       -23.51063       287.02997       0.28038       13.20725       0.07181       1.63673       0.25       H         1901       4       -23.27581       246.73026       0.24526       13.01772       0.07307       1.8111       0.25       H										
1789 4 -23.51063 287.02997 0.28038 13.20725 0.07181 1.63673 0.25 H 1901 4 -23.27581 246.73026 0.24526 13.01772 0.07307 1.8111 0.25 H										
1901 4 -23.27581 246.73026 0.24526 13.01772 0.07307 1.8111 0.25 H										

Table A2 – continued from previous page

Table A2 – continued from previous page									
GroupID	Nm	$M_{r,G}$	$\sigma$	$R_{harm}$	log M	$t_C$	$\log\! ho$	$f_{sp}$	Class
1532	4	-23.48681	290.3558	0.3017	13.24909	0.07638	1.54125	0.25	Н
382	4	-23.66696	235.03648	0.25684	12.99559	0.08033	1.75098	0.0	Н
1551	4	-23.05234	218.18669	0.23852	12.89883	0.08036	1.84741	0.25	Н
2225	5	-23.31458	271.63577	0.29852	13.1866	0.08079	1.65197	0.4	Н
2295	4	-23.13318	379.60504	0.41893	13.62446	0.08113	1.11354	0.25	Н
1487	4	-23.21317	236.5384	0.26164	13.00915	0.08131	1.72688	0.25	Н
2263	7	-24.03493	309.5383	0.34409	13.36175	0.08172	1.61299	0.43	Н
2067	5	-23.32188	187.8088	0.22045	12.73439	0.08629	2.04698	0.2	H
1779	4	-24.19759	349.39413	0.44331	13.57699	0.09327	1.03984	0.25	Н
737	4	-23.46191	182.11754	0.23148	12.72887	0.09344	1.88643	0.25	Н
1764	4	-23.34622	186.03825	0.24803	12.77735	0.098	1.79648	0.0	Н
533	4	-23.43282	205.0583	0.27449	12.90593	0.0984	1.66439	0.25	Н
2284	4	-22.62204	182.58755	0.25591	12.77468	0.10303	1.75571	0.0	Н
1341	4	-24.649	227.4405	0.32053	13.06326	0.1036	1.46235	0.0	Н
2102	4	-24.14641	192.48509	0.27218	12.8473	0.10395	1.67541	0.0	Н
2099	4	-23.58294	249.14816	0.35999	13.19286	0.10622	1.31109	0.0	Н
1044	4	-23.70229	205.87936	0.30124	12.9498	0.10756	1.54321	0.25	Н
1681	4	-23.29212	184.97379	0.32199	12.88571	0.12796	1.45646	0.0	H
1388	4	-23.85669	197.21857	0.38342	13.01723	0.14292	1.22893	0.5	H
2239	4	-23.62445	217.1688	0.44853	13.16904	0.15182	1.02461	0.25	Н

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